



# Beam Loss Simulations at injection plateau

Giuliano Franchetti

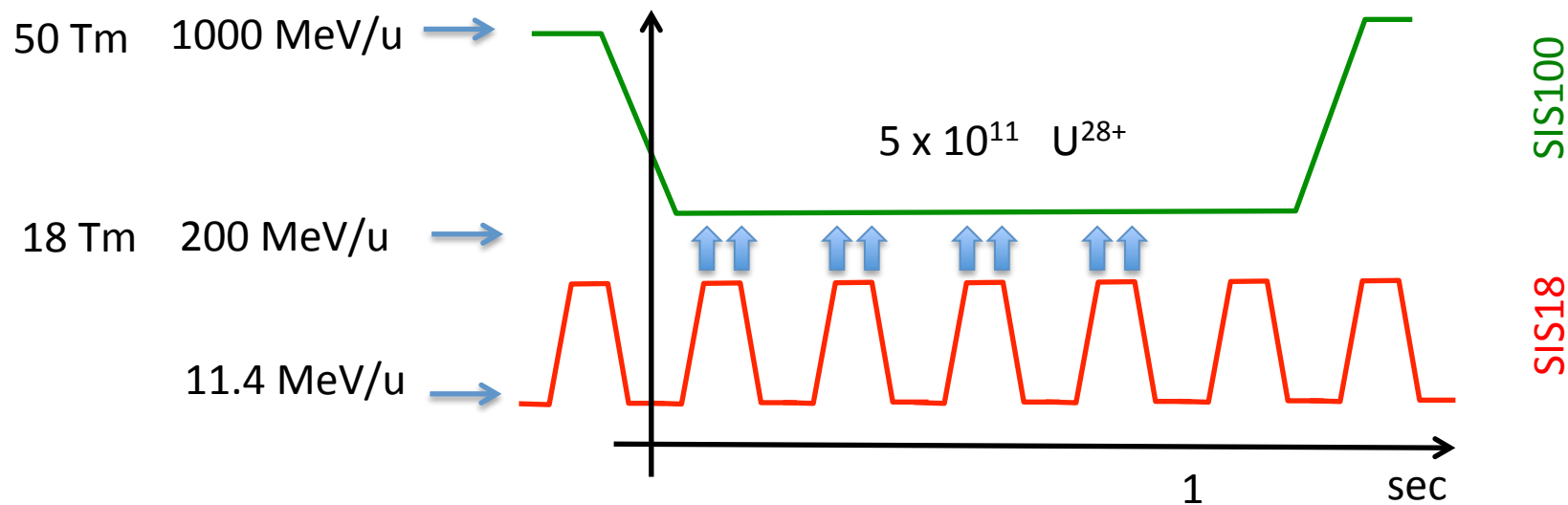
MAC 2010

1-2 December 2010

# Overview

- **SIS100 injection plateau scenario**
- **Beam Loss Mechanism Mechanism**
- **Beam Loss Prediction for SIS100**
- **Improving Beam Loss**
- **Robustness of the correction scheme**
- **Next Step: Verification in SIS18**
- **Conclusion and Final Remarks**

# SIS100 injection plateau scenario



## First bunch @ 200 MeV/u

Nominal  $N_{\text{ions}} = 6.25 \times 10^{10}/\text{bunch}$

Beam1:  $\epsilon_{x/y} = 35/15 \text{ mm-mrad } (2\sigma) \Delta Q_{x/y} = -0.21/-0.33$

Beam2:  $\epsilon_{x/y} = 50/20 \text{ mm-mrad } (2\sigma) \Delta Q_{x/y} = -0.15/-0.24$

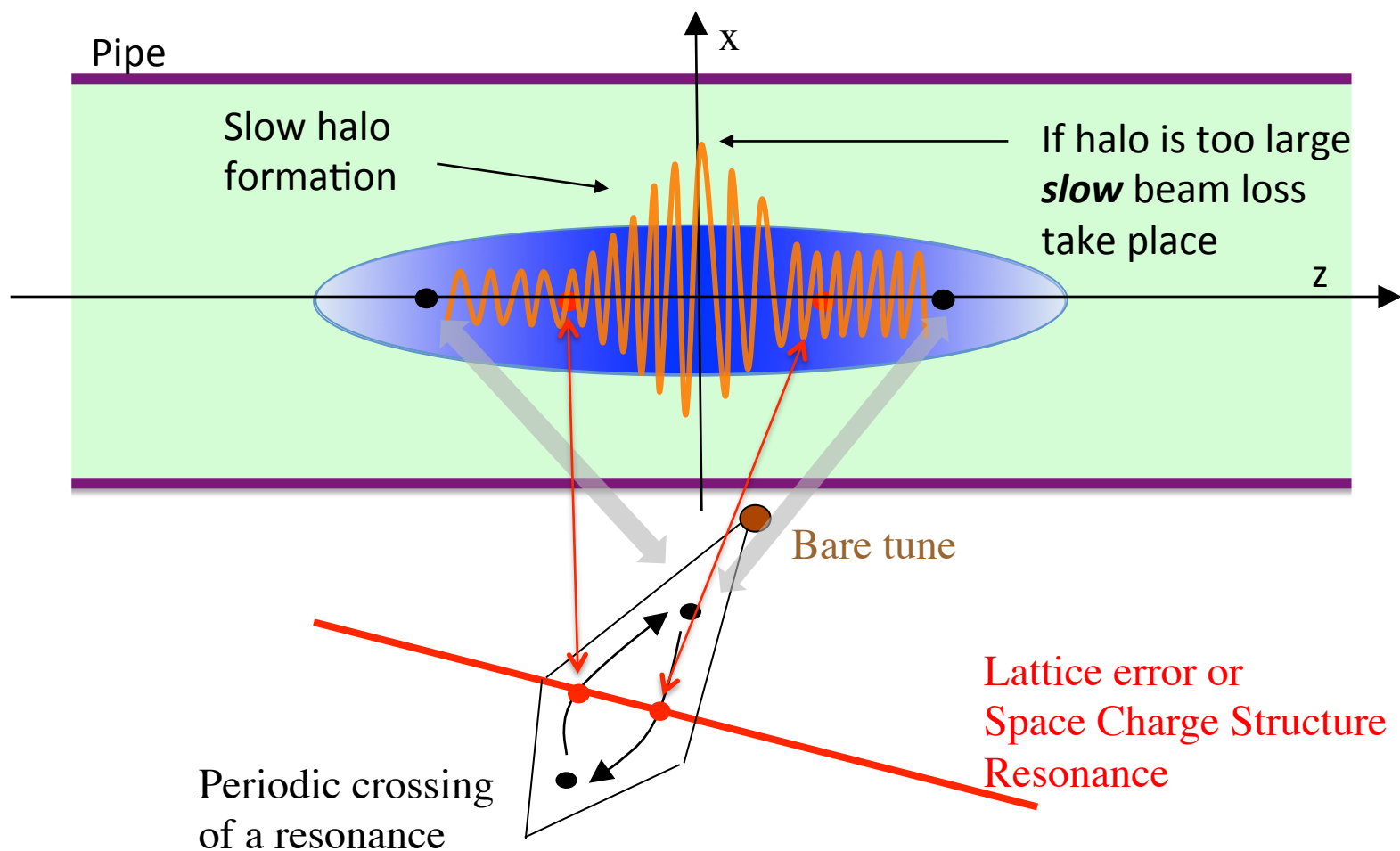
Turns =  $1.57 \times 10^5$  (1 sec.)

**Problem of control of beam loss for the bunched beams in SIS100 during 1 second**



# BEAM LOSS MECHANISM

# Mechanism of beam loss



# Key ingredients

- 1) Space charge tune-spread
- 2) Lattice Resonance
- 3) Longitudinal motion (bunched beam)



Halo amplitude and speed of halo formation has a complex dependence from

- 1) Space charge incoherent tune-shift
- 2) Position of bare tune with respect to the resonance
- 3) Strength of the resonance
- 4) Longitudinal profile



# Experimental verification in SIS18

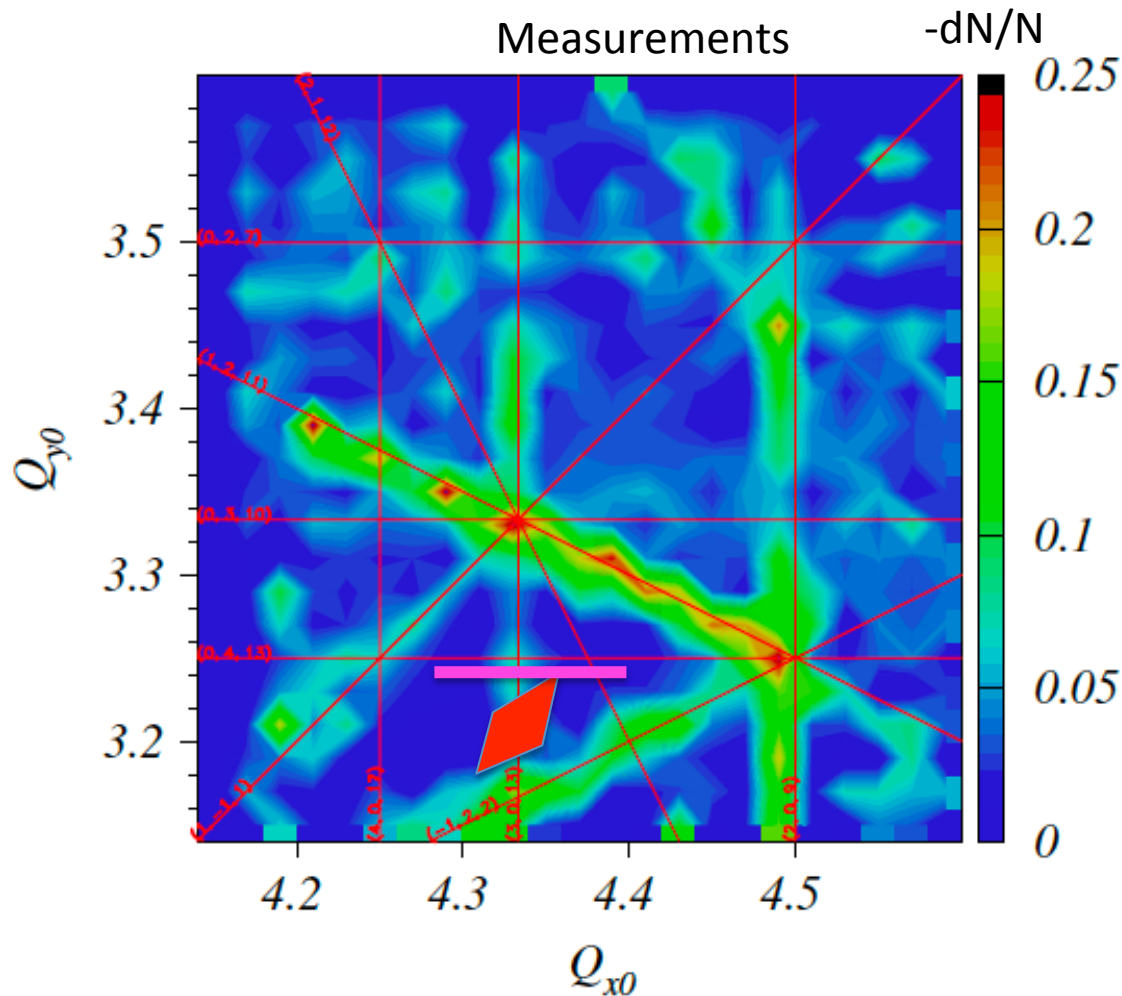


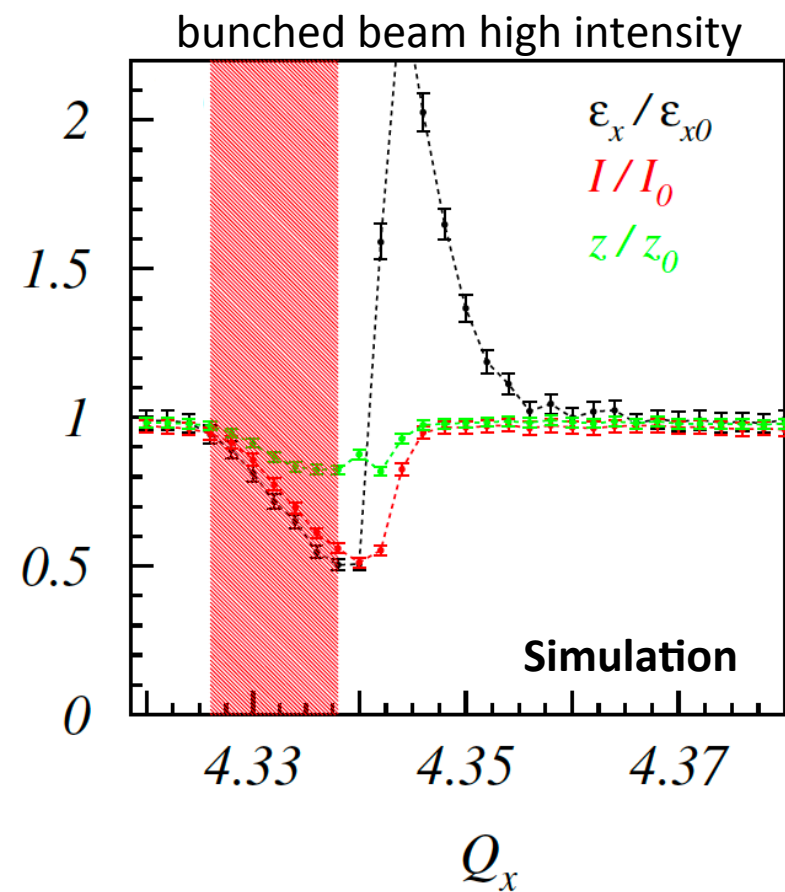
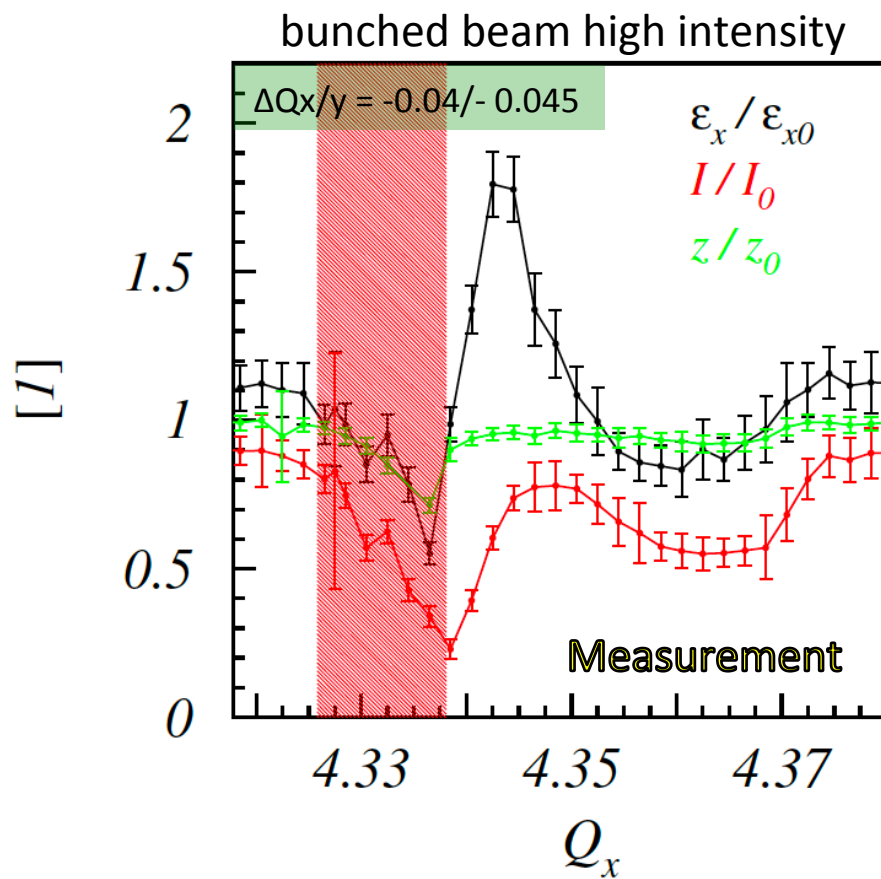
TABLE I. Typical parameters of SIS18 and of the ion beam used.

Parameter	Value	Units
Energy per nucleon	11.28	MeV/u
Ion mass number	40	
Ion charge state	18	
rf harmonics	4	
rf voltage	4	kV
Total particles per bunch	$3.125 \times 10^8$	
Gamma transition	5.01	
Rigidity	1.077	Tm
SIS18 circumference	216.1	m
Average $\beta_x$	$\sim 8$	m
Average $\beta_y$	$\sim 10$	m
Revolution time	4.673	$\mu\text{s}$
Eta transition	0.9362	
Synchrotron tune	$6.915 \times 10^{-3}$	
Bunching factor	0.3357	
Rms momentum spread	$1.3 \times 10^{-3}$	
Bunch length $4\sigma$	560	ns
Maximum $\delta p/p$ in the bucket	$7.4 \times 10^{-3}$	
Horizontal emittance at $2\sigma$	19	mm mrad
Vertical emittance at $2\sigma$	14	mm mrad
Horizontal peak tune shift	$-4 \times 10^{-2}$	
Vertical peak tune shift	$-4.5 \times 10^{-2}$	

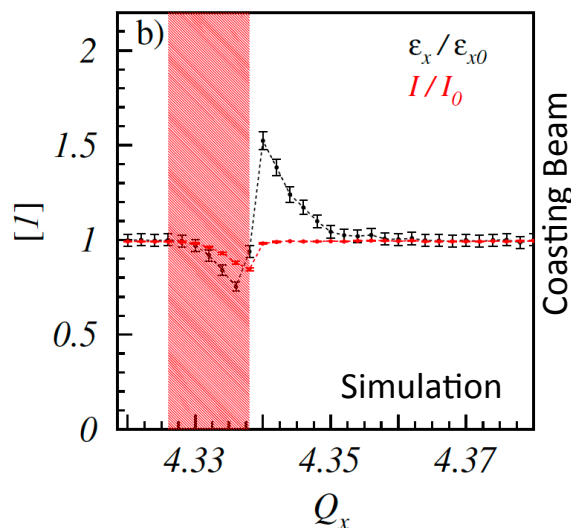
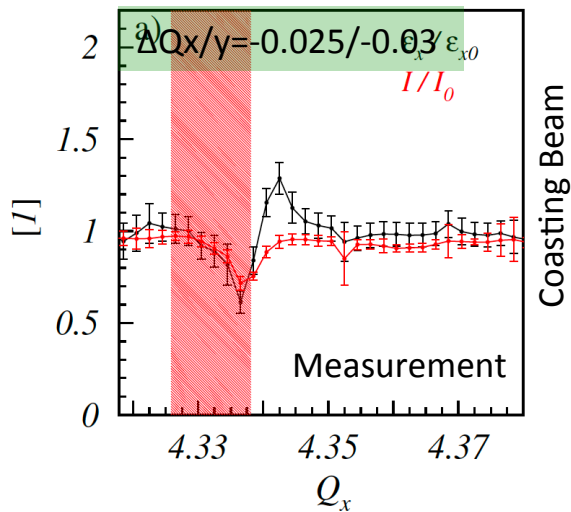
G. Franchetti et al., GSI-Acc-Note-2005-02-001

# Experimental verification in SIS18

G. Franchetti, O. Chorniy, I. Hofmann, W. Bayer, F. Becker, P. Forck, T. Giacomini, M. Kirk, T. Mohite, C. Omet, A. Parfenova, and P. Schuett PRSTAB **13**, 114203 (2010)







## Simulations made with MICROMAP library

- Full linear and nonlinear optics;
- Symplectic tracking;
- Frozen space for long term tracking: analytic Model for a Gaussian Transverse-Longitudinal beam distribution;
- PIC available, but not used for  $10^5$  turns (!) for avoiding noise effects on beam.

The library has been tested against codes  
for the self-consistent part

+

Tested against the SIS18 measurements (benchmarking)

# SUMMARY

Experimental evidence show that slow beam loss takes place only when the following 3 elements are simultaneously present

- 1) Space charge tune-spread
- 2) Lattice Resonance
- 3) Longitudinal motion (bunched beam)

**MICROMAP predicts beam loss a factor 2 less than real beam loss**



# BEAM LOSS PREDICTION FOR SIS100

# SIS100 Modeling

- 1) Linear Lattice
- 2) All insertions (i.e. each element sizes + all septums, NO Collimators)
- 3) Each magnet has nonlinear field modeled via 3 localized nonlinear kicks of the systematic errors
- 4) Displacement of quadrupoles is modeled by insertion of a dipolar kick in center of quadrupole
- 5) Inclusion of all magnet correctors: steerers and sextupole for chromatic correction and resonance corrector sextupoles (in addition with quadrupoles and octupoles)

Magnet design: CSLD *Pavel Akishin, Anna Mierau, Pierre Schnizer, Egbert Fischer 3. June 2010*

Magnet multipoles: *V.Kapin, P. Schnizer, A. Mierau*

*Kapin, V.; Franchetti, G. ACC-note-2010-004*

Lattice: *J. Stadlmann, A. Parfenova, S.Sorge*

# SIS100 magnet nonlinearities

## Multipoles in magnets up to order 15: nonlinear kick in Entrance Body Exit

### EXAMPLE

#### Dipole: Body

#### Quadrupole: Body

!===== the dipole model 25/6/2010 =====

```
!SIS100_Dipole_CSLD8b
!"Rogovsky_I1_1319kA_Cntr_Bpho_Tm_10.17_CO_xy_p0.0_p0.0_mm"
!"data_hdf/SIS100_Dipole_CSLD_Harmonics_20100609.h5:
!/Dipole/D3/Curved/CSLD8b/Rogovsky_Profile/"
MDC0 MULTIPOLE -4.8321734468527902E-02 -8.0460622403658862E-11 0
MDC1 MULTIPOLE 1.3222876973075998E-06 -4.4286349322627113E-09 1
MDC2 MULTIPOLE -1.5411882617349000E-02 -2.6132592908204184E-07 2
MDC3 MULTIPOLE -3.7034493848285333E-03 -1.8587012098560845E-05 3
MDC4 MULTIPOLE 4.5506880778861124E+01 2.9261019441204273E-04 4
MDC5 MULTIPOLE -6.2559995183645212E+00 2.3583431753596007E-01 5
MDC6 MULTIPOLE 7.3051033143311797E+04 -1.4162812922709435E+02 6
MDC7 MULTIPOLE -1.4288951062831108E+05 -3.4965239042733432E+04 7
MDC8 MULTIPOLE 2.2831975374350262E+09 1.0324892588690210E+07 8
MDC9 MULTIPOLE 1.0564506501167362E+10 2.9113326625993242E+09 9
MDC10 MULTIPOLE -1.6359949140068581E+14 -7.0591807199292908E+11 10
MDC11 MULTIPOLE -6.9868819985378656E+13 -2.1251269228490359E+14 11
MDC12 MULTIPOLE 2.5207268897163274E+18 3.4255809404212480E+16 12
MDC13 MULTIPOLE 1.6101150642536155E+19 1.1090489334002389E+19 13
MDC14 MULTIPOLE -2.2667622204271218E+23 -9.5935636945850047E+20 14
MDC15 MULTIPOLE -8.9215833271142267E+22 -3.2804988706914617E+23 15
```

!===== model of quadrupole 25/6/2010 =====

```
!SIS100_Quadrupole6Turn
!"Quad6TurnsV1_I1_460kA_Cntr_Bpho_Tm_12.23_CO_xy_p0.0_p0.0_mm"
!"data_hdf/SIS100_Quadrupole6Turn_20100623.h5:
!/Quadrupole/Turns6/D3/OperaCalc/StaticCalculation/V1/"
Eqb0 MULTIPOLE -2.6789881018894428E-14 5.5045898388867806E-14 0
Eqb1 MULTIPOLE 2.1717022154679769E-01 1.9856320529300420E-12 1
Eqb2 MULTIPOLE -9.4521226576819973E-11 1.9401448718616971E-10 2
Eqb3 MULTIPOLE 3.7858283188846437E-03 1.0501181037334316E-08 3
Eqb4 MULTIPOLE 7.0414842692841817E-07 -1.4318783375984776E-06 4
Eqb5 MULTIPOLE 3.0194294633632222E+02 -2.8051263507461471E-04 5
Eqb6 MULTIPOLE -7.8478544512944073E-02 1.6019533278747095E-01 6
Eqb7 MULTIPOLE -1.8269515944715394E+06 2.5709785026550517E+01 7
Eqb8 MULTIPOLE 4.7775705574752483E+03 -9.7507153716628163E+03 8
Eqb9 MULTIPOLE 1.5853417177689340E+11 -1.7429770135777944E+06 9
Eqb10 MULTIPOLE -2.5512932132258266E+08 5.2083611876728094E+08 10
Eqb11 MULTIPOLE -6.9973814030639240E+15 9.9896489034391388E+10 11
Eqb12 MULTIPOLE 9.8111951662325020E+12 -2.0032780989903805E+13 12
Eqb13 MULTIPOLE 1.2725759662788647E+20 -4.1250219682152360E+15 13
Eqb14 MULTIPOLE -2.1305597834814832E+17 4.3518970770377338E+17 14
Eqb15 MULTIPOLE -8.7801330870650991E+23 9.4854103306132488E+19 15
```



# SIS100 working point and lattice resonances

Resistive wall instability

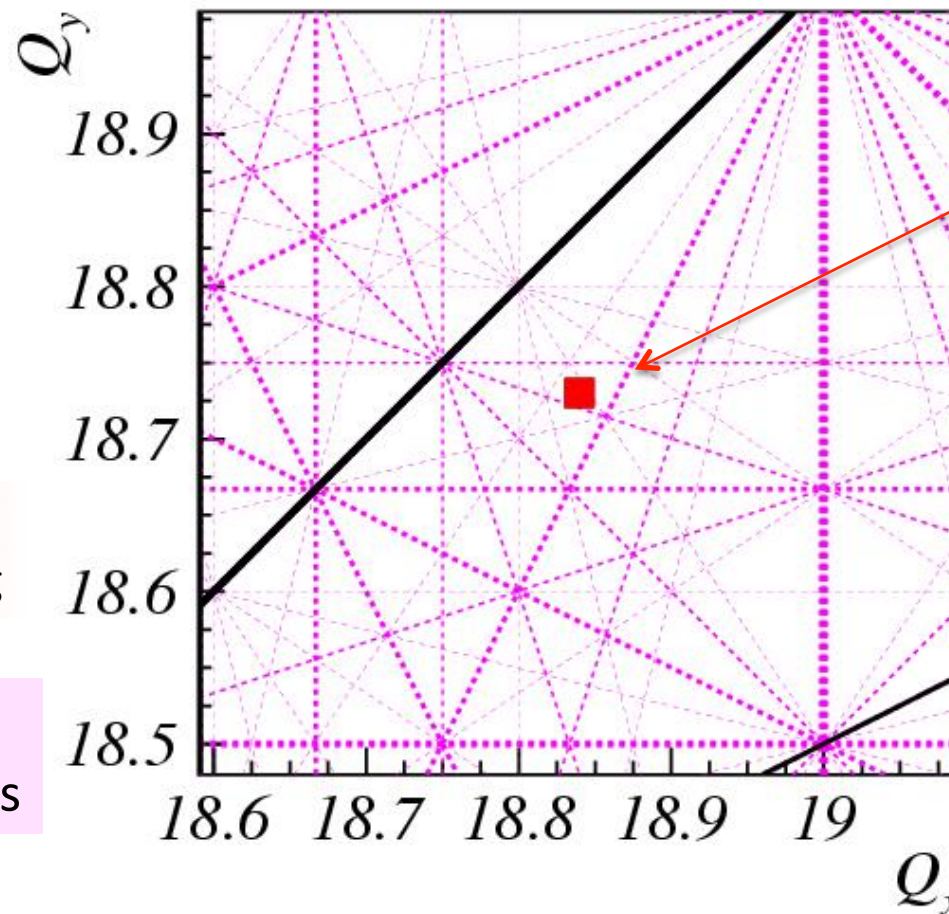
Montague stop-band must be avoided

Space charge induced periodic resonance crossing

Systematic resonances

Random resonances

$Q_x = 18.84, Q_y = 18.73$



SIS100 working point

*I. Hofmann, G. Franchetti, GSI report 2005*  
*G. Franchetti et al., EPAC 2006*



# Random Errors and COD

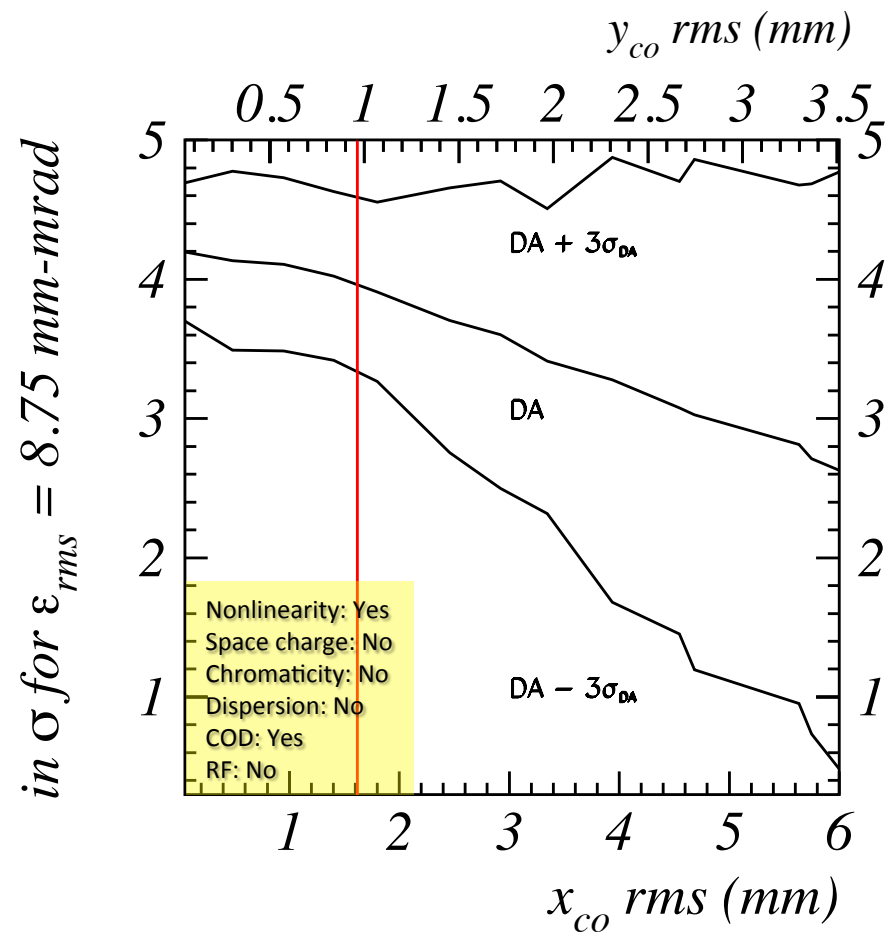
In order to predict beam loss we have to consider the effect of random deviation of systematic multipolar components in magnets

We call “seed” one sequence of random errors in SIS100 magnets + COD

**Random error:** Taken as 30% of the systematic component (Gaussian distribution)

**COD:** is obtained by adding a thin dipole in the quad of random strength  $\delta K_0 = 1.6 \times 10^{-5}$  rad.  
This value is consistent with a rms COD of 1mm obtained after correcting the closed orbit deformation

# Effect of random error and COD

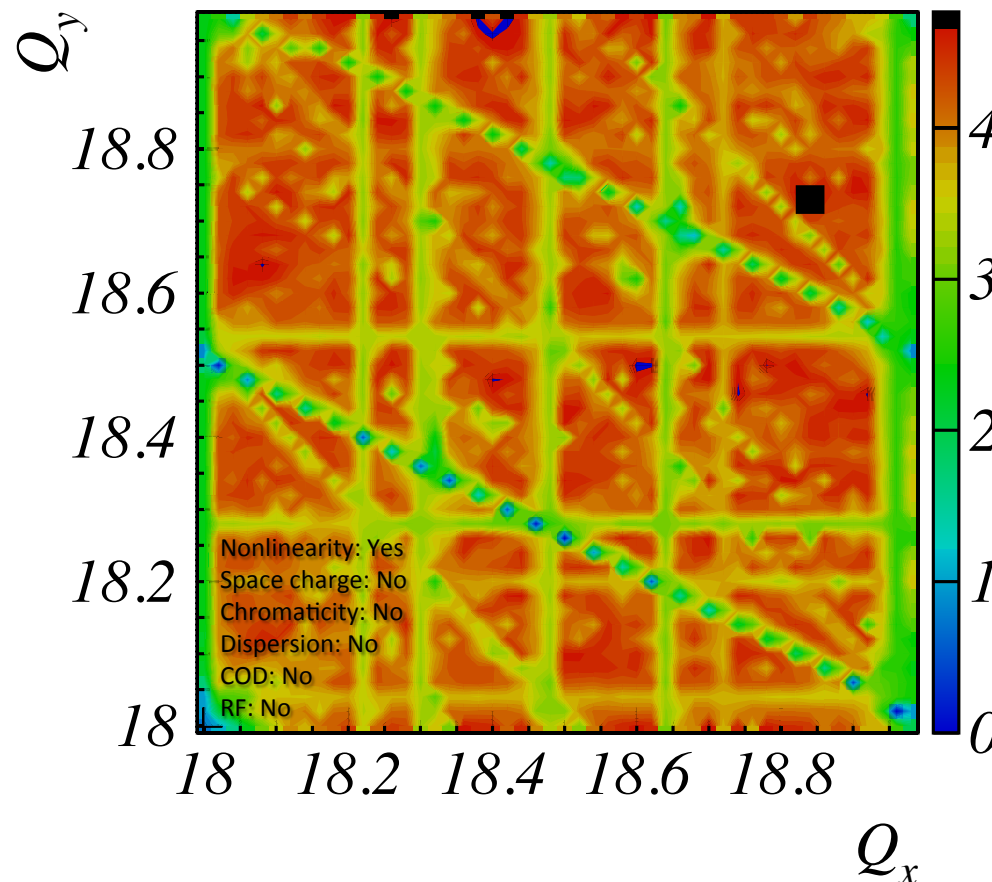


In absence of random error  
DA =  $4.8 \sigma$

# Random errors, DA, and Resonances

## Statistical view of the possible resonances

$$[\langle DA \rangle - 3 \text{ st.dev.}(DA)]/\sigma$$



Short term DA (1000 turns)

Average DA – 3 standard dev !

Statistics on 30 error seeds  
of random errors and  
quadrupoles displacement

NO COD included in these  
simulations

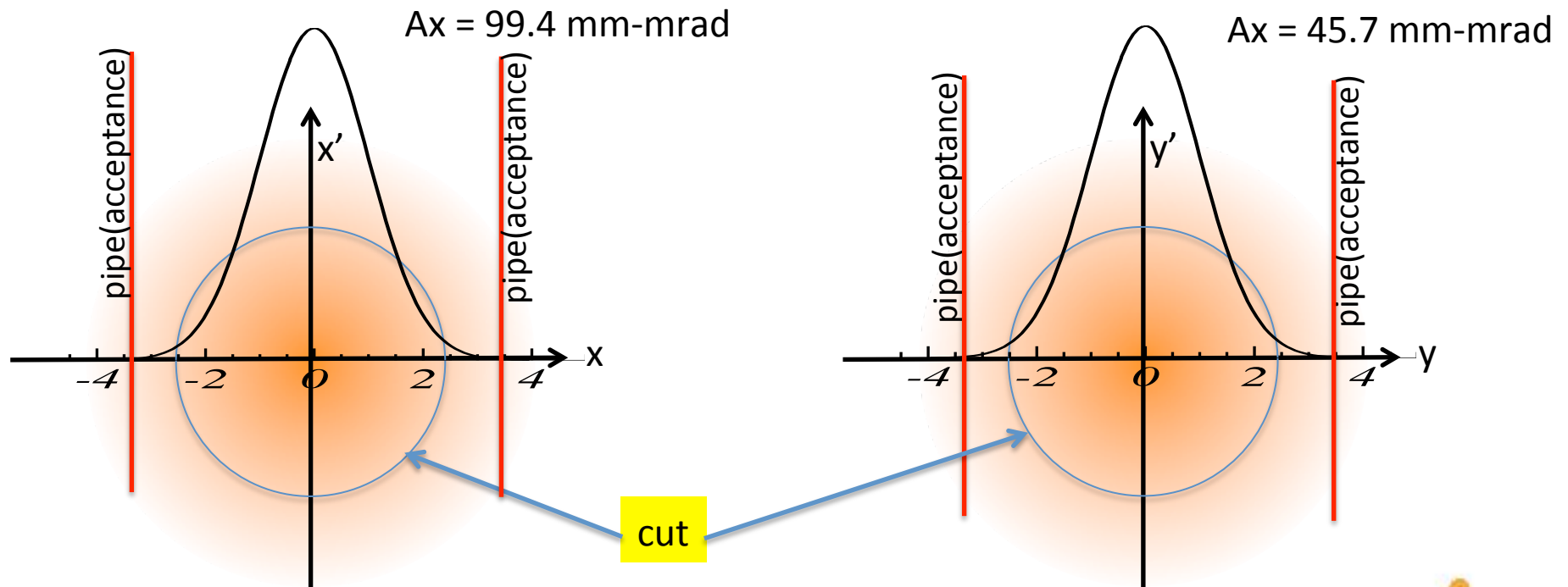
# Simulations: Beam Properties

The distribution is truncated in energy, in each plane, at 2.5 sigma

Beam1:  $\epsilon_{x2\sigma} = 35$  mm-mrad,  $\epsilon_{y2\sigma} = 15$  mm-mrad

Beam2:  $\epsilon_{x2\sigma} = 50$  mm-mrad,  $\epsilon_{y2\sigma} = 20$  mm-mrad

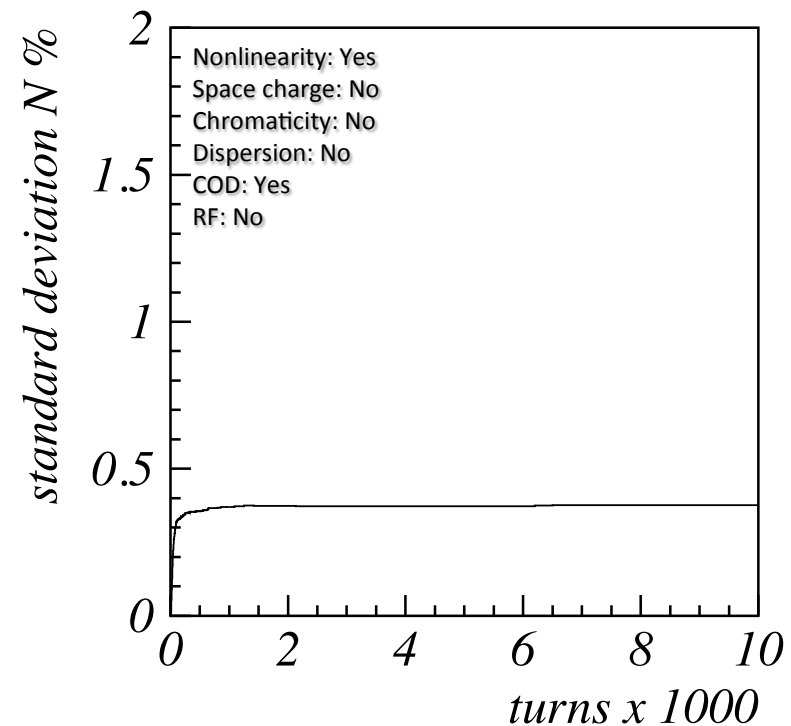
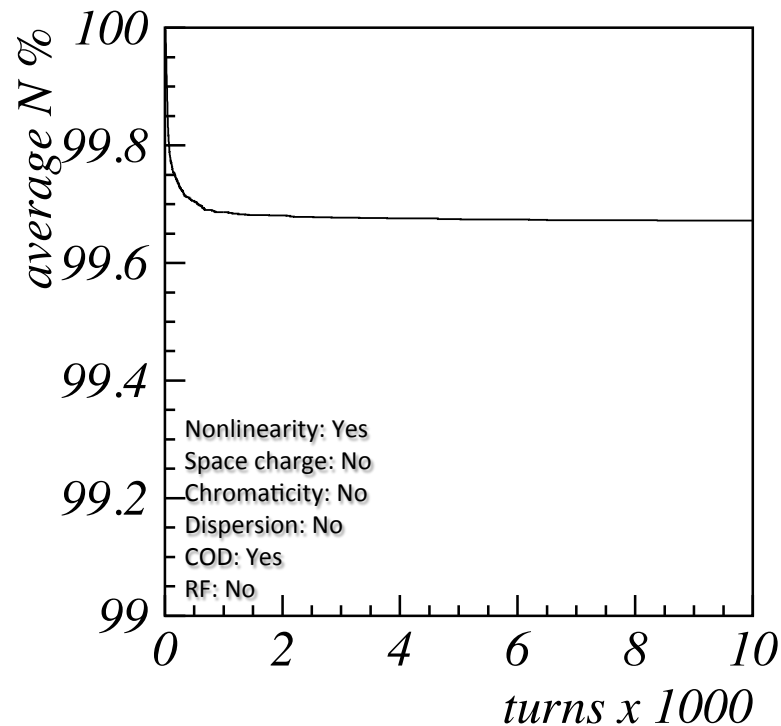
Particle distribution is Gaussian, matched with the lattice and injected 1mm off center



# Identification of the “standard error seed”

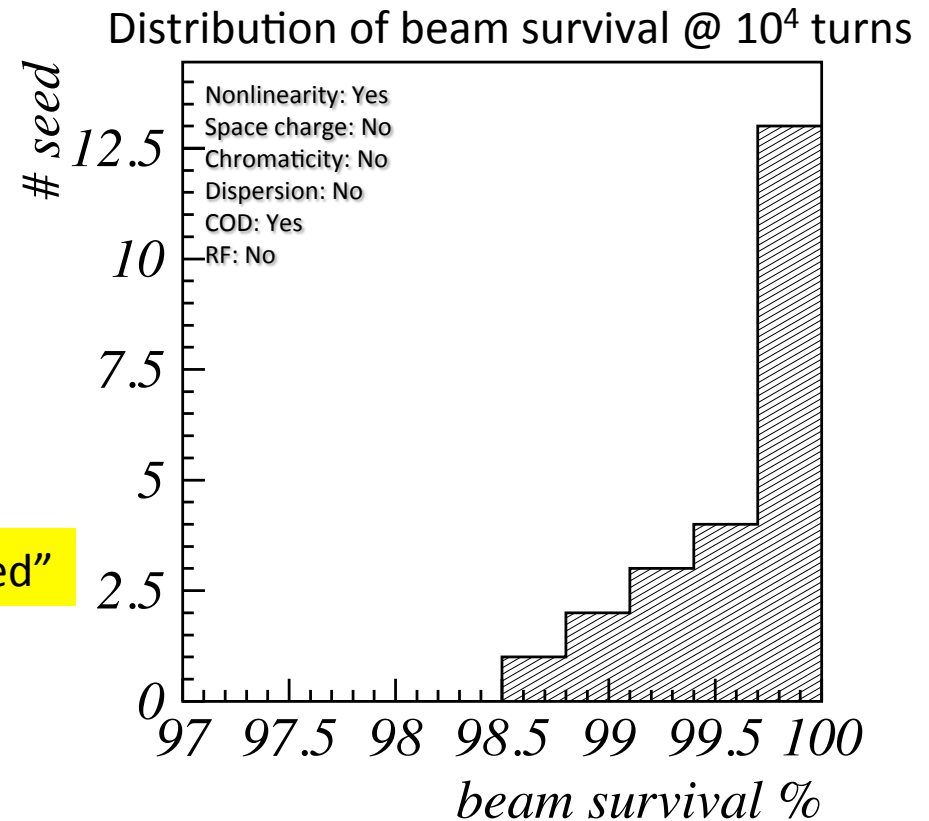
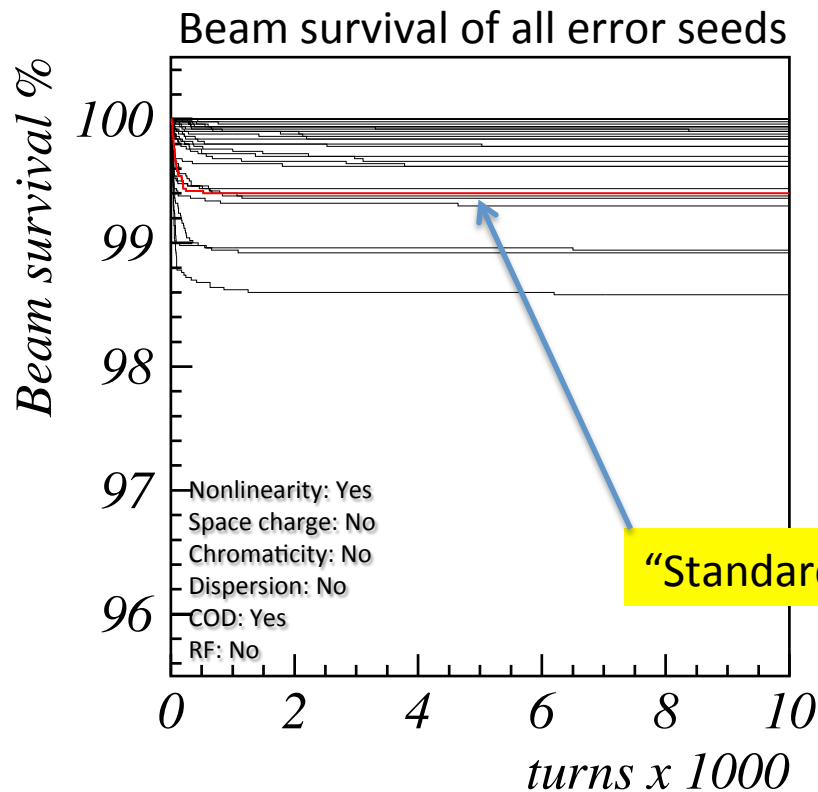
Beam used: **Beam2**  
5000 macro-particles  
Statistics over 30 seeds

No Chromaticity  
No Dispersion



# Choice of the “standard seed”

To select the error standard error seed we use the **Beam2** as a probe



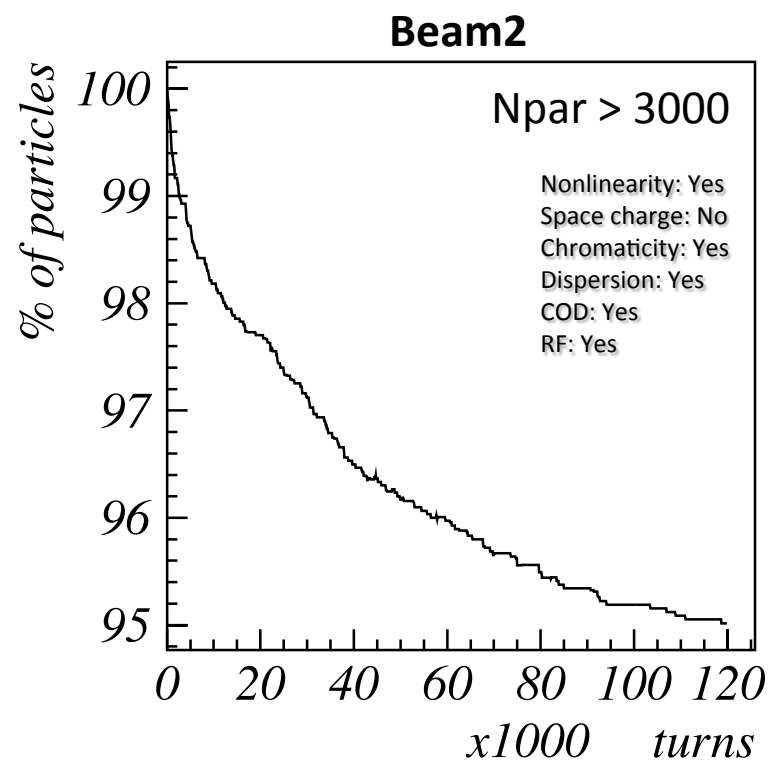
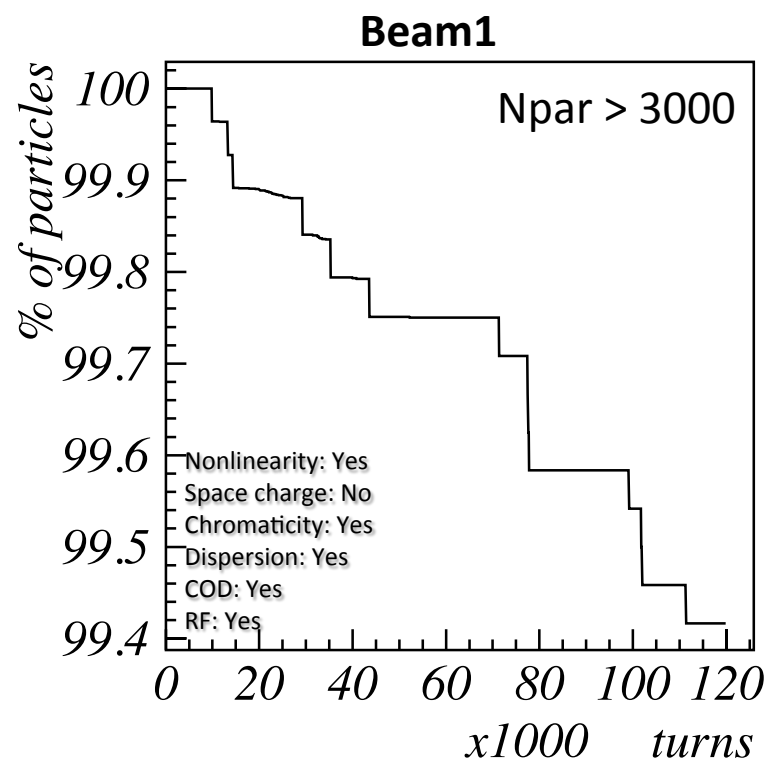


# Check over full cycle length

bunch length +/- 90°  
Bf = 0.35

$(\delta p/p)_{\text{rms}} = \pm 5 \times 10^{-4}$   
 $1/Q_s = 233$  turns

Simulation extended  
to  $1.57 \times 10^5$  turns



# Including space charge

We investigate here only Beam 1

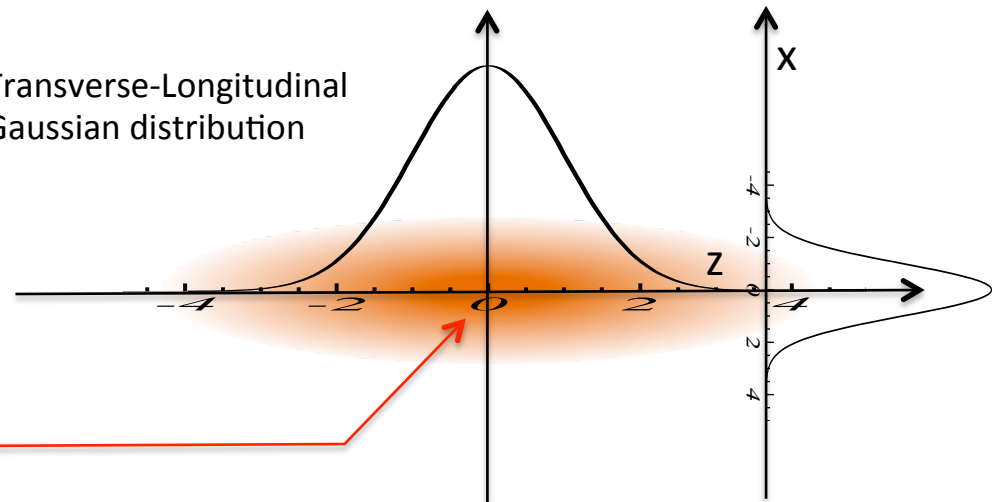
Beam1:  $\Delta Q_{x/y} = -0.217 / -0.334$  (-0.2106/ -0.371) @  $0.625 \times 10^{11}$  particles per bunch  
 Beam2:  $\Delta Q_{x/y} = -0.154 / -0.245$  @  $0.625 \times 10^{11}$  particles per bunch

From FFT in the code:  
 the difference stems from the effect of  
 the optics on beam envelope

$$\Delta Q_{x,sc} = \frac{\bar{\beta}_x}{2} R_{acc} \frac{K_{peak}}{\sqrt{\bar{\beta}_x \epsilon_x} (\sqrt{\bar{\beta}_x \epsilon_x} + \sqrt{\bar{\beta}_y \epsilon_y})}$$

$$\Delta Q_{y,sc} = \frac{\bar{\beta}_y}{2} R_{acc} \frac{K_{peak}}{\sqrt{\bar{\beta}_y \epsilon_y} (\sqrt{\bar{\beta}_x \epsilon_x} + \sqrt{\bar{\beta}_y \epsilon_y})}$$

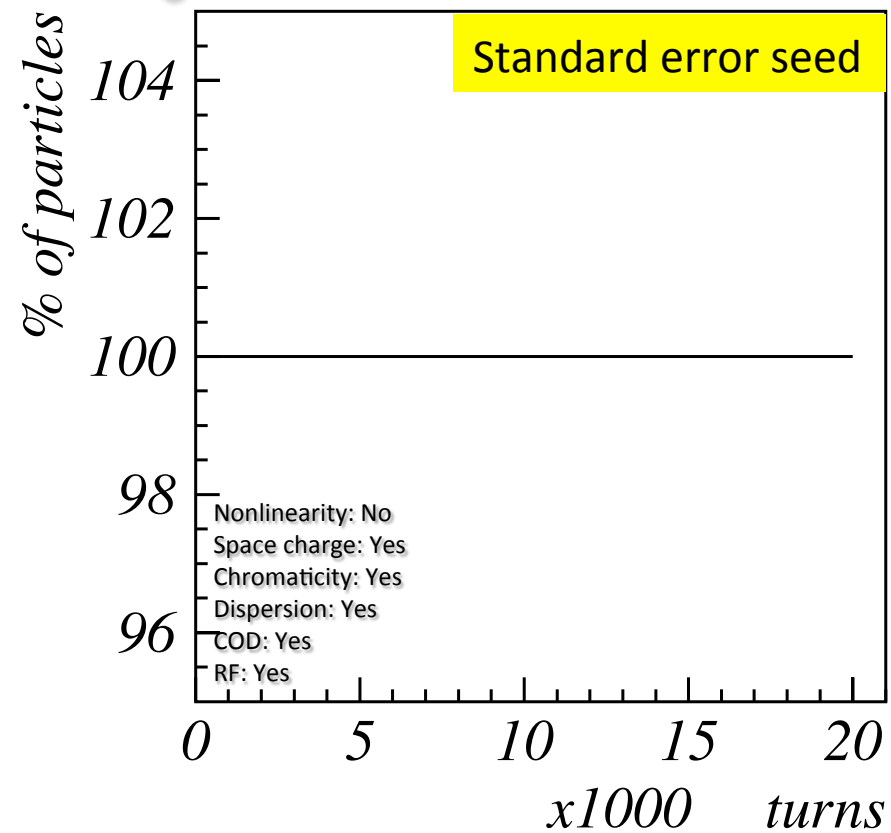
Transverse-Longitudinal  
 Gaussian distribution



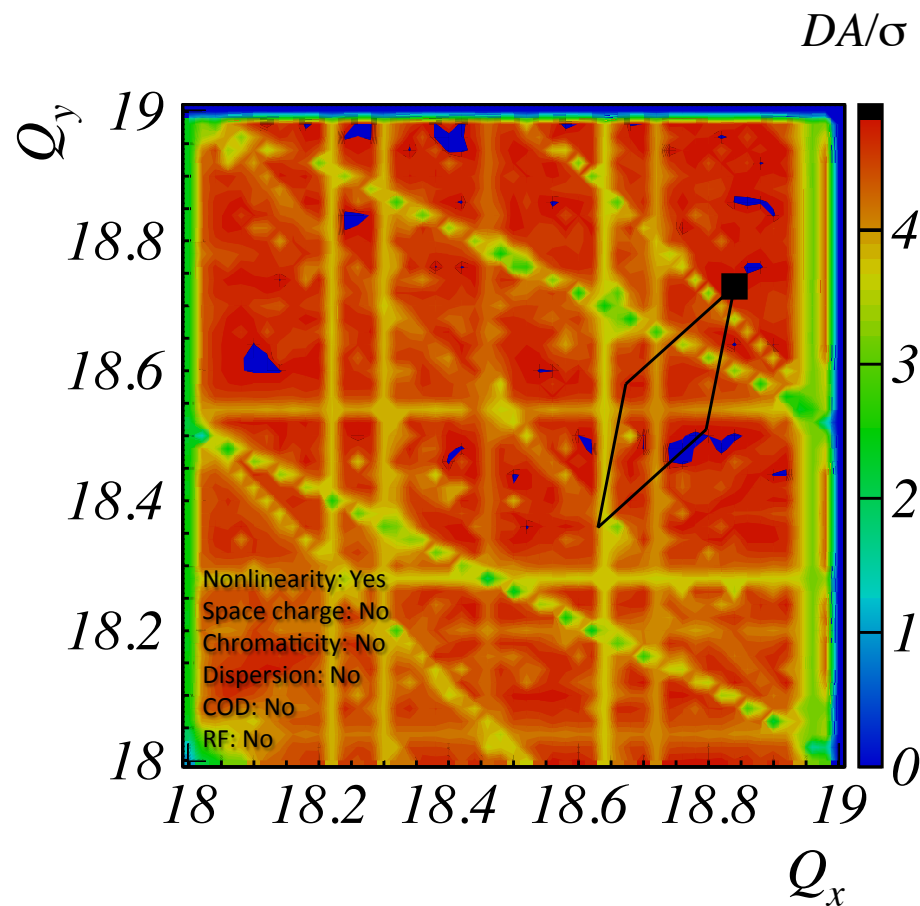
Tuneshift

# Does the space charge create a trouble without nonlinearities ?

Answer: **NO**



# Resonances excited by the “standard seed”



Resonances crossing the  
space charge tune-spread

$$2 Q_y = 37$$

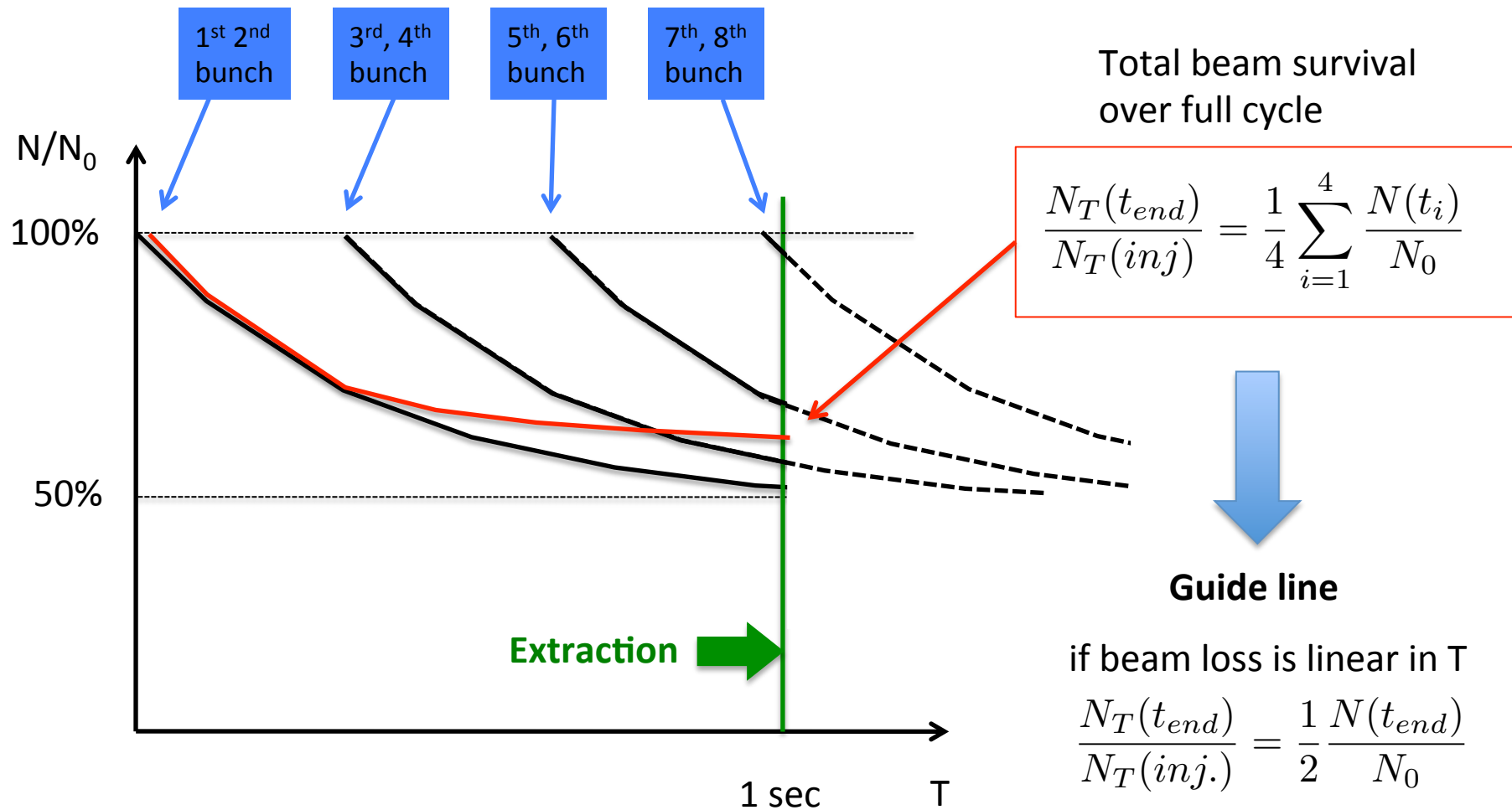
$$Q_x + 2 Q_y = 56$$

$$3 Q_x = 56$$

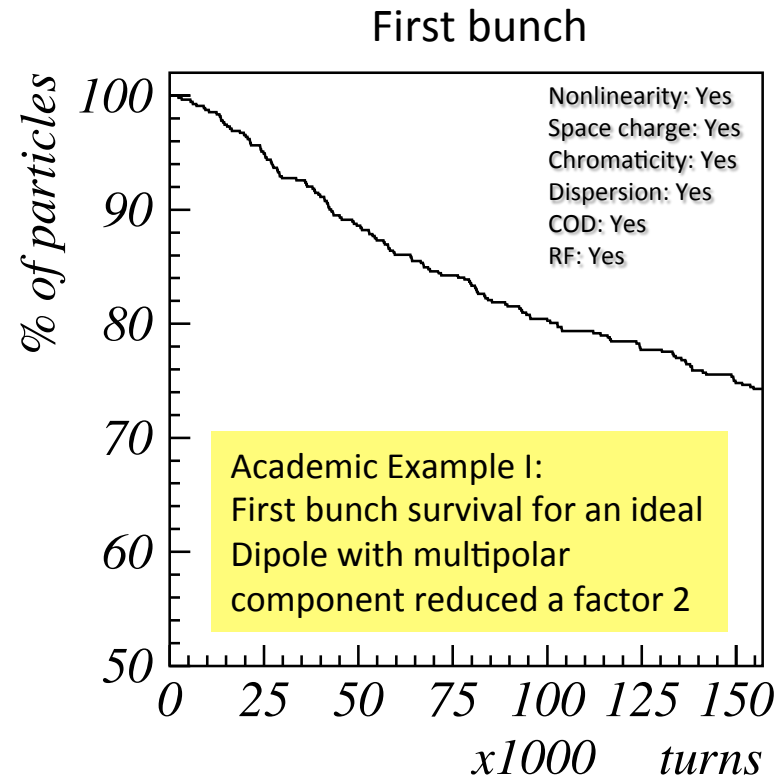
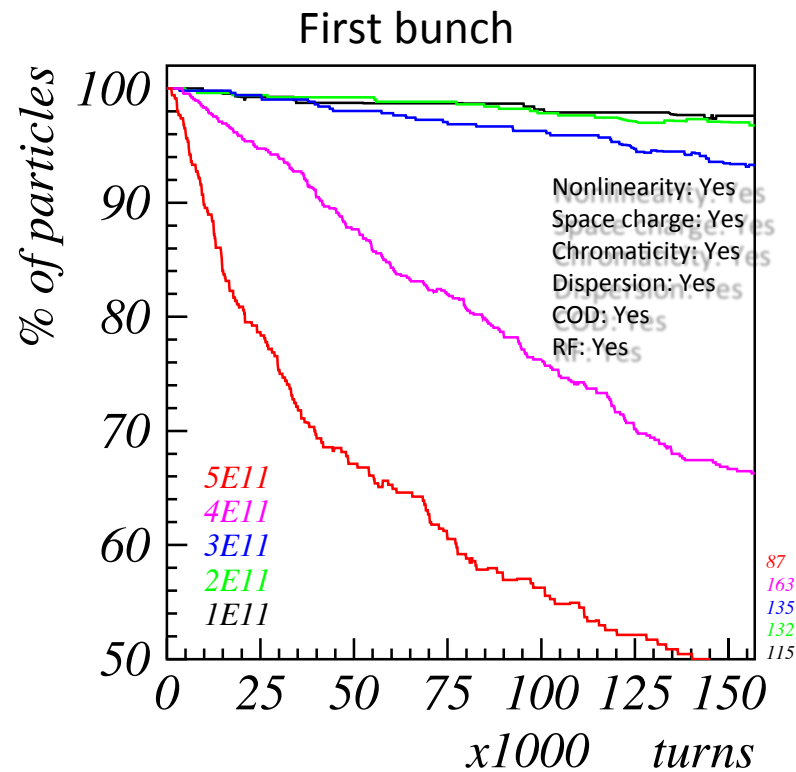
$$2 Q_x + 2 Q_y = 75$$

$$4 Q_x = 75$$

# Relation between beam survival over full cycle and survival of 1<sup>st</sup> bunch



# Beam loss versus beam intensity

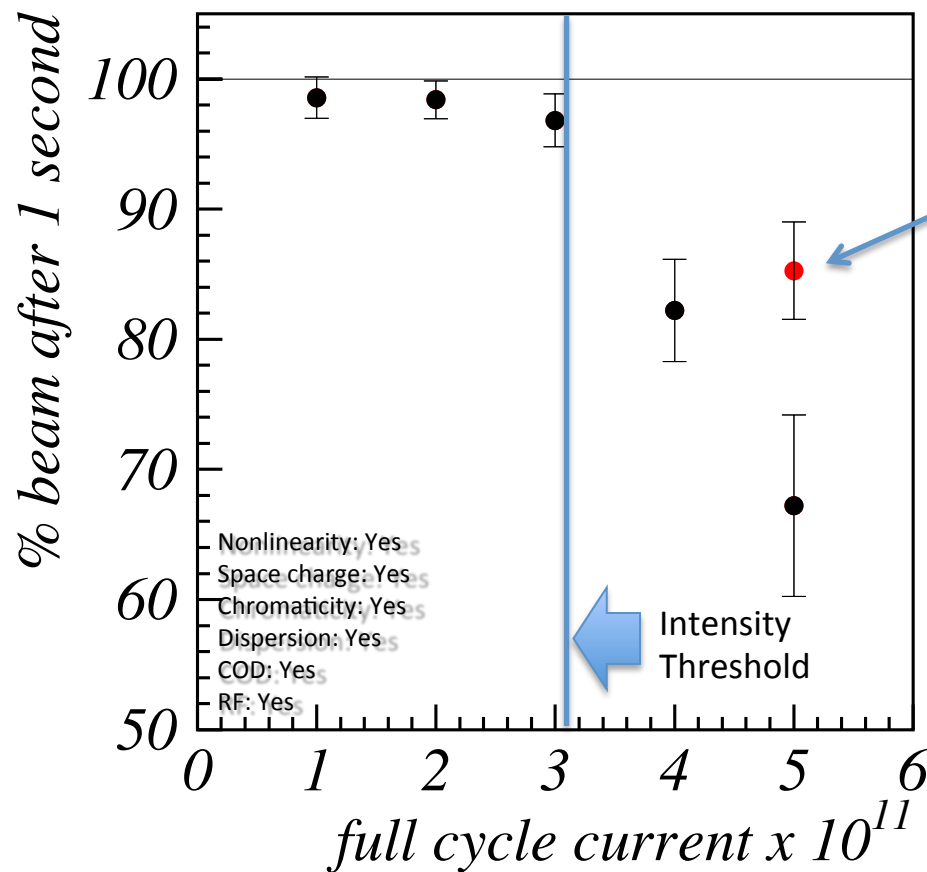


Clear indication that beam intensity is relevant for beam survival but also that magnet nonlinearities are relevant in the beam loss budget



# A global view: performances vs. intensity

$$\varepsilon_{x/y,2\sigma} = 35/15 \text{ mm-mrad}$$



## Academic example I

This results suggests that dipoles with better quality enhance beam lifetime

**But**

Using the physical understanding of the beam loss mechanism we can try to control beam loss

# SUMMARY

## For the “standard error” seed

Beam loss are strongly affected by space charge: for intensities below  $3E11$  beam loss are contained within 5%

At maximum beam intensity  $5E11$  beam loss over the full cycle is 35%

Improvement of all multipolar components improve beam loss to 15%

**How do we use the understanding of the mechanism of beam loss to control them ?**

**In TDR2008 it was suggested that  $Q_x + 2Q_y = 56$  might be responsible of beam loss  
[also suggested in G.Franchetti et al. PRSTAB 12, 124401 (2009)]**

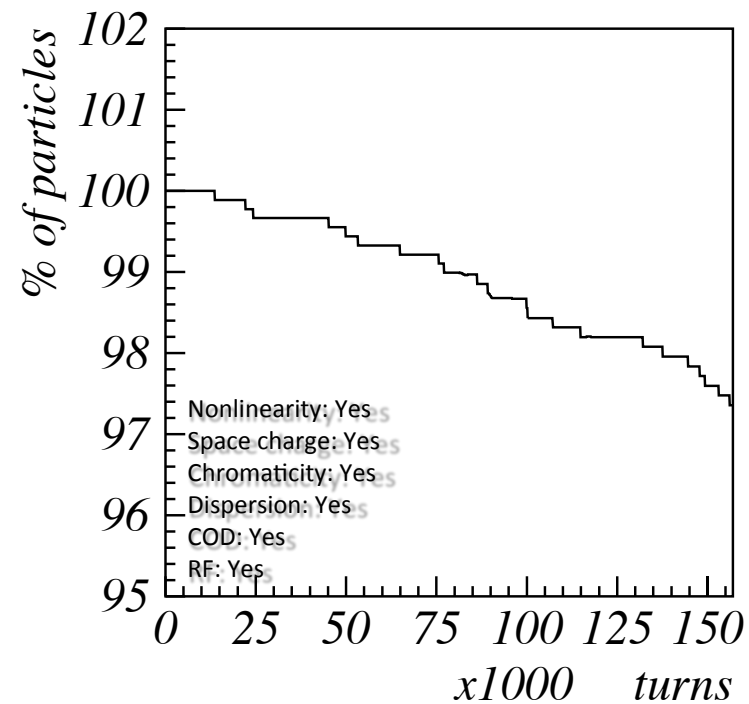
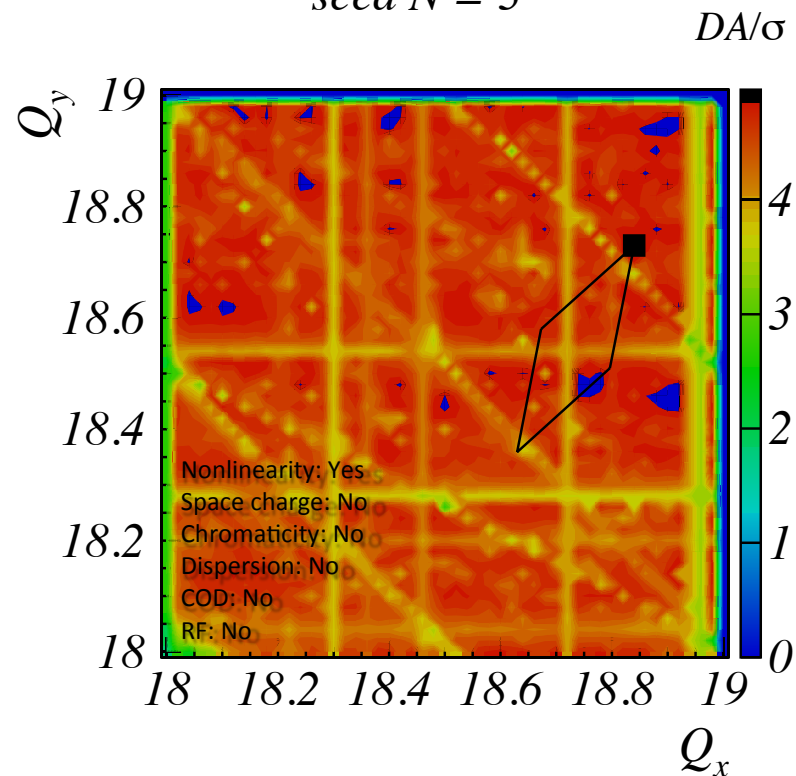


# IMPROVING BEAM LOSS

# Academic example II

We remove the 3<sup>rd</sup> order components from dipoles

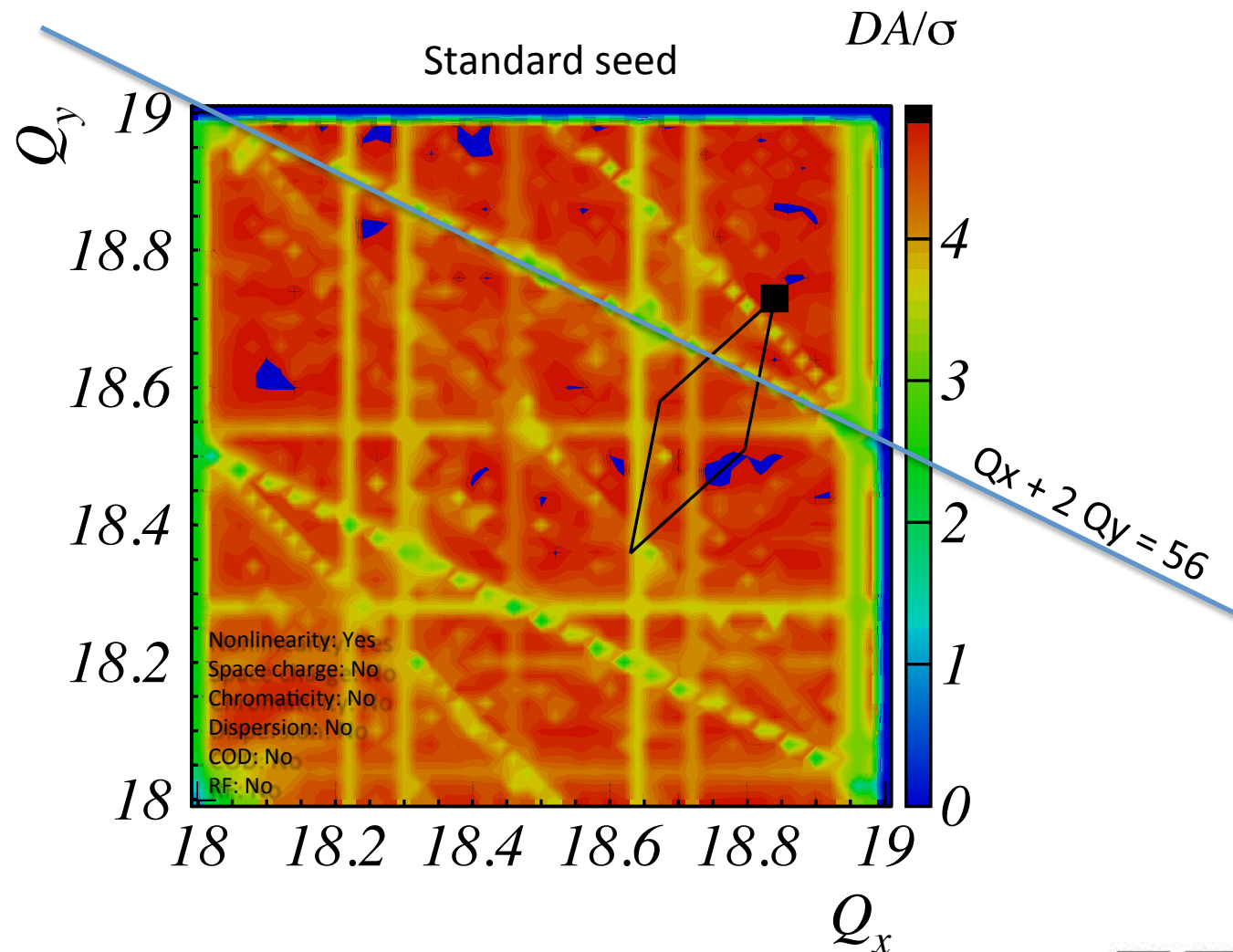
seed  $N = 3$



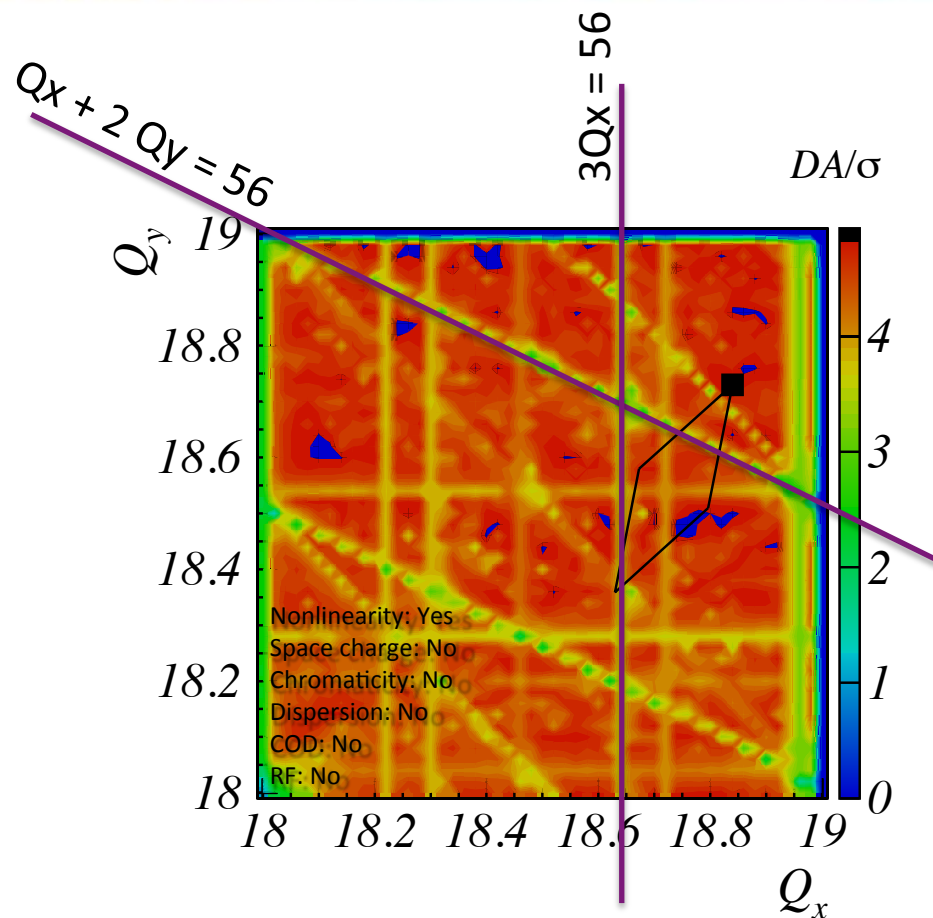
3<sup>rd</sup> order resonances are practically absent: only 4<sup>th</sup> order resonances dominates

First bunch beam survival is good, but this is an academic example

# Does resonance compensation really mitigate periodic crossing diffusion ?



# Compensation Strategy: A first approach



Compensate the resonance  
 $Q_x + 2 Q_y = 56$   
 without exciting the resonance  
 $3 Q_x = 56$



## Compensation strategy

Cancellation of the driving terms of  
 $Q_x + 2 Q_y = 56$  and  $3 Q_x = 56$   
 at the crossing of the two resonances  
 that we call "cancellation working point"

WPC:  $Q_{xc} = 18.66$ ,  $Q_{yc} = 18.66$



# Analysis of the driving terms

## General expression of the driving terms


G. Guignard CERN 78-11 10 November 1978


$$h = \frac{R}{2\pi(2R)^{N/2}|n_x!||n_y!|} \sum_j \beta_{xj}^{|n_x|/2} \beta_{yj}^{|n_y|/2} \times e^{i[n_x \phi_{xj} + n_y \phi_{yj} - (n_x Q_x + n_y Q_y - p)s_j/R]} \begin{cases} (-1)^{(|n_y|+2)/2} K_{N,j} \text{ for } n_y \text{ even} \\ (-1)^{(|n_y|-1)/2} J_{N,j} \text{ for } n_y \text{ odd} \end{cases}$$

We define  $k_{N,j}$  to be associated to  $K_{N,j}$

$$k_{N,j} = \frac{R}{2\pi(2R)^{N/2}|n_x!||n_y!|} \beta_{xj}^{|n_x|/2} \beta_{yj}^{|n_y|/2} \times e^{i[n_x \phi_{xj} + n_y \phi_{yj} - (n_x Q_x + n_y Q_y - p)s_j/R]} \begin{cases} (-1)^{(|n_y|+2)/2} \text{ for } n_y \text{ even} \\ (-1)^{(|n_y|-1)/2} \text{ for } n_y \text{ odd} \end{cases}$$

$$h = \sum_l k_{2,l} K_{2,l} + \sum_j k_{2,j} K_{2,j}$$

This term depends only on the nonlinear errors:  we call it  $k_{\text{error}}$

This term depends only on the correctors 

We consider only normal sextupolar components

# Correction system normalized driving terms

The normalized resonance driving terms  $k_{2,j} = |k_{2,j}|e^{i\theta}$  at the “cancellation point”  
 $Q_{xc} = Q_{yc} = 18.66$  follow the symmetry of the optics

WPC:  $Q_{xc} = 18.667$   $Q_{yc} = 18.667$

**Resonance**      **3 Qx = 56**

**Kerr =**      **-3.53E-03 + i5.30E-04**

Nele	$ k_{2,j} $	$\vartheta/(2\pi)$
1	1.02E-02	0.5
535	5.36E-02	1.3963
2494	1.02E-02	1.8333
3028	5.36E-02	2.7297
4987	1.02E-02	3.1667
5513	5.36E-02	4.063
7472	1.02E-02	4.5
7998	5.36E-02	5.3963
9957	1.02E-02	5.8333
10483	5.36E-02	6.7297
12442	1.02E-02	7.1667
12986	5.36E-02	8.063

WPC:  $Q_{xc} = 18.667$   $Q_{yc} = 18.667$

**Resonance**      **Qx + 2 Qy = 56**

**Kerr =**      **9.63E-03 + i 3.26E-03**

Nele	$ k_{2,j} $	$\vartheta/(2\pi)$
1	8.93E-02	0
535	5.28E-02	0.89866
2494	8.93E-02	1.3333
3028	5.28E-02	2.232
4987	8.93E-02	2.6667
5513	5.28E-02	3.5653
7472	8.93E-02	4
7998	5.28E-02	4.8987
9957	8.93E-02	5.3333
10483	5.28E-02	6.232
12442	8.93E-02	6.6667
12986	5.28E-02	7.5653

# Full scheme of assigning 4 independent strengths

We have created 4 knobs,  $b_1, b_2, b_3, b_4$  assigning to the 12 sextupoles the following values

Nele	Name strength	Name object	value
1	$K_{2,1}^2$	corr_oct1	$b_3$
535	$K_{2,1}^1$	corr_oct2	$b_1$
2494	$K_{2,2}^2$	corr_oct3	$b_3$
3028	$K_{2,2}^1$	corr_oct4	$b_1$
4987	$K_{2,3}^2$	corr_oct5	$-b_3$
5513	$K_{2,3}^1$	corr_oct6	$-b_1$
7472	$K_{2,4}^2$	corr_oct7	$b_4$
7998	$K_{2,4}^1$	corr_oct8	$b_2$
9957	$K_{2,5}^2$	corr_oct9	$-b_4$
10483	$K_{2,5}^1$	corr_oct10	$-b_2$
12442	$K_{2,6}^2$	corr_oct11	$b_4$
12986	$K_{2,6}^1$	corr_oct12	$b_2$

EFFECT on Chromaticity

$$\left| \frac{\partial Q_{x/y}}{\partial(\delta p/p)} \right| < \frac{1}{\pi} \beta_{x,max} D_{x,max} |b_i|_{max}$$

This strategy allows the minimization of the strength to be applied to the 12 strength in order to control DA

# Application to the “standard error seed”

Therefore the simultaneous compensation of  $Q_x + 2 Q_y = 56$  and  $3 Q_x = 56$  reads

$$\begin{aligned} & -0.35349 \times 10^{-2} + i0.52999 \times 10^{-3} + \\ & + (k_{2,1}^1 + k_{2,2}^1 - k_{2,3}^1)b_1 + (k_{2,4}^1 - k_{2,5}^1 + k_{2,6}^1)b_2 \\ & + (k_{2,1}^2 + k_{2,2}^2 - k_{2,3}^2)b_3 + (k_{2,4}^2 - k_{2,5}^2 + k_{2,6}^2)b_4 = 0 \end{aligned}$$

with  $k_{2,I}^l$  computed  
for  $3 Q_x = 56$  @ WPC

$$\begin{aligned} & 0.96308 \times 10^{-2} + i0.32631 \times 10^{-2} + \\ & + (k_{2,1}^1 + k_{2,2}^1 - k_{2,3}^1)b_1 + (k_{2,4}^1 - k_{2,5}^1 + k_{2,6}^1)b_2 \\ & + (k_{2,1}^2 + k_{2,2}^2 - k_{2,3}^2)b_3 + (k_{2,4}^2 - k_{2,5}^2 + k_{2,6}^2)b_4 = 0 \end{aligned}$$

with  $k_{2,I}^l$  computed  
for  $Q_x + 2 Q_y = 56$  @ WPC

This is a system of 4 equation in the 4 unknown  $b_1, b_2, b_3, b_4$

For the seed #3 we find

$$\begin{aligned} b_1 &= -0.0523366015 \quad m^{-3} \\ b_2 &= -0.0250475799 \quad m^{-3} \\ b_3 &= -0.0307216893 \quad m^{-3} \\ b_4 &= -0.0214847964 \quad m^{-3} \end{aligned}$$



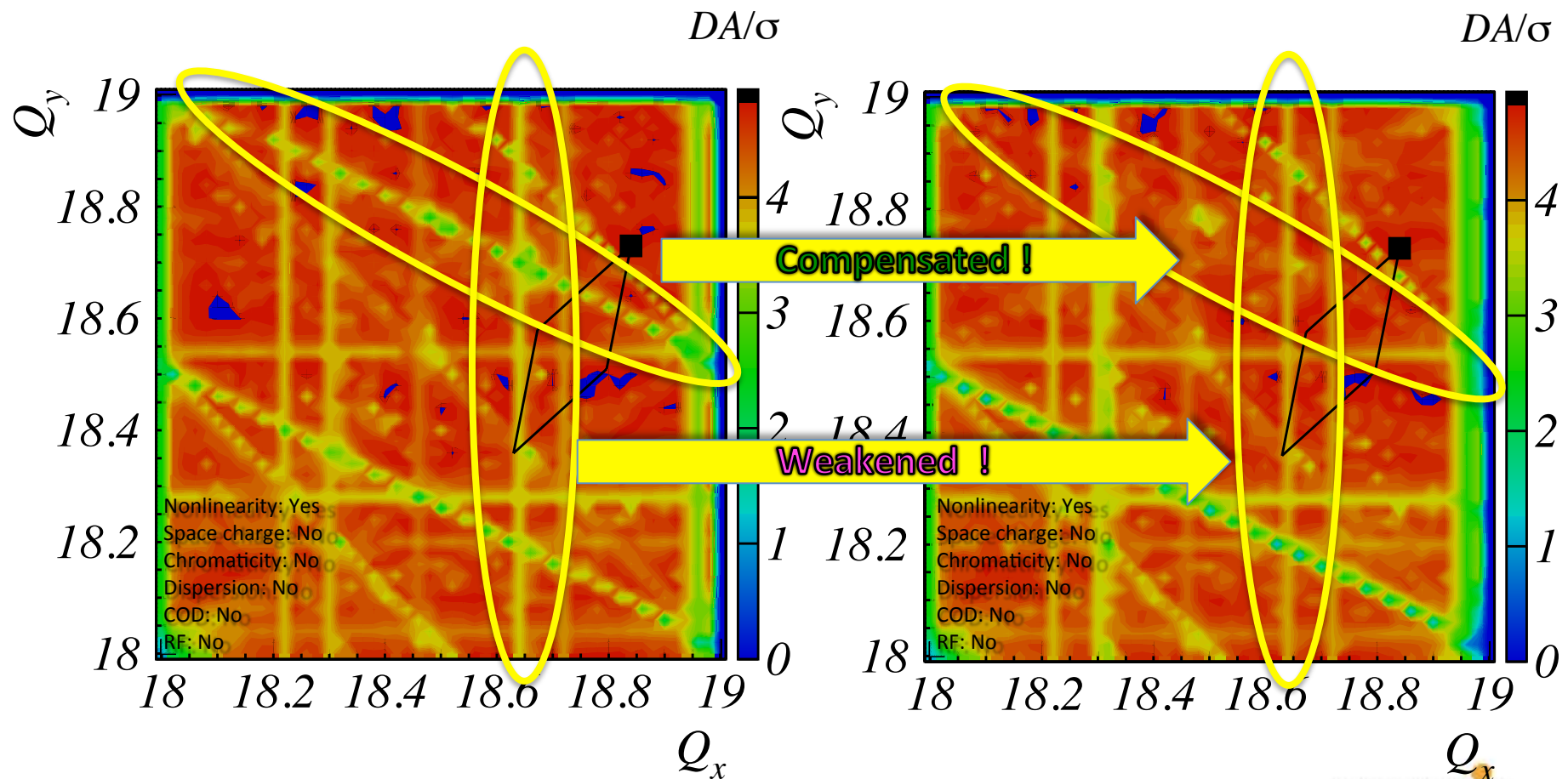
Negligible effect  
on chromaticity

$$\left| \frac{\partial Q_{x/y}}{\partial(\delta p/p)} \right| < 0.04$$

# DA scan verification

Resonances from standard error seed

including compensation compensation



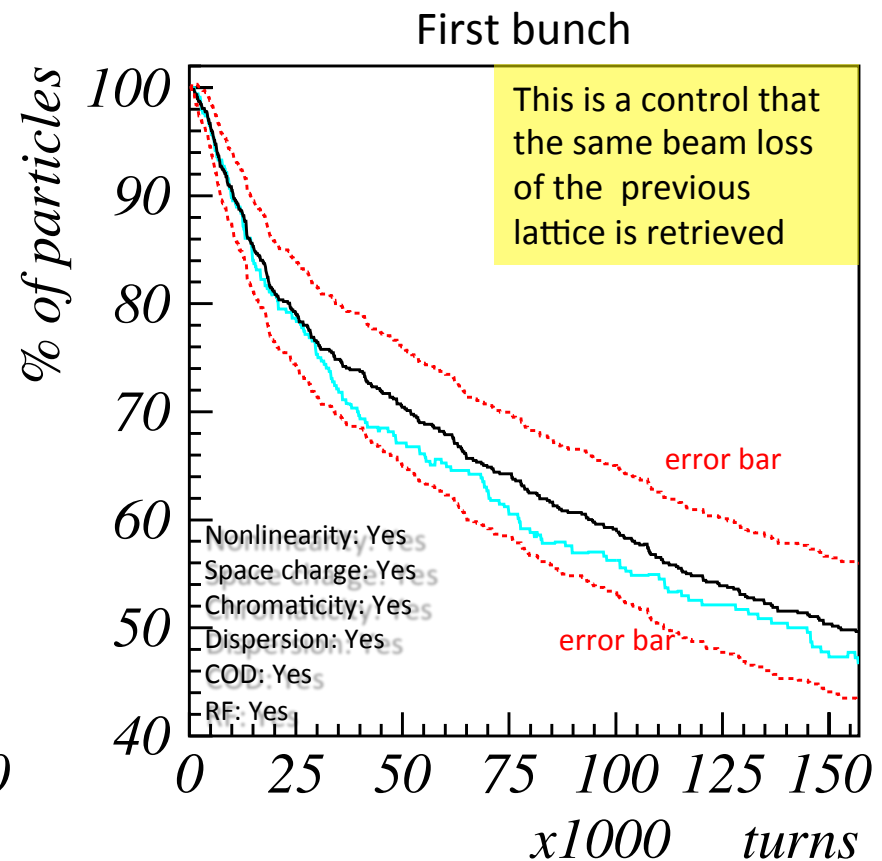
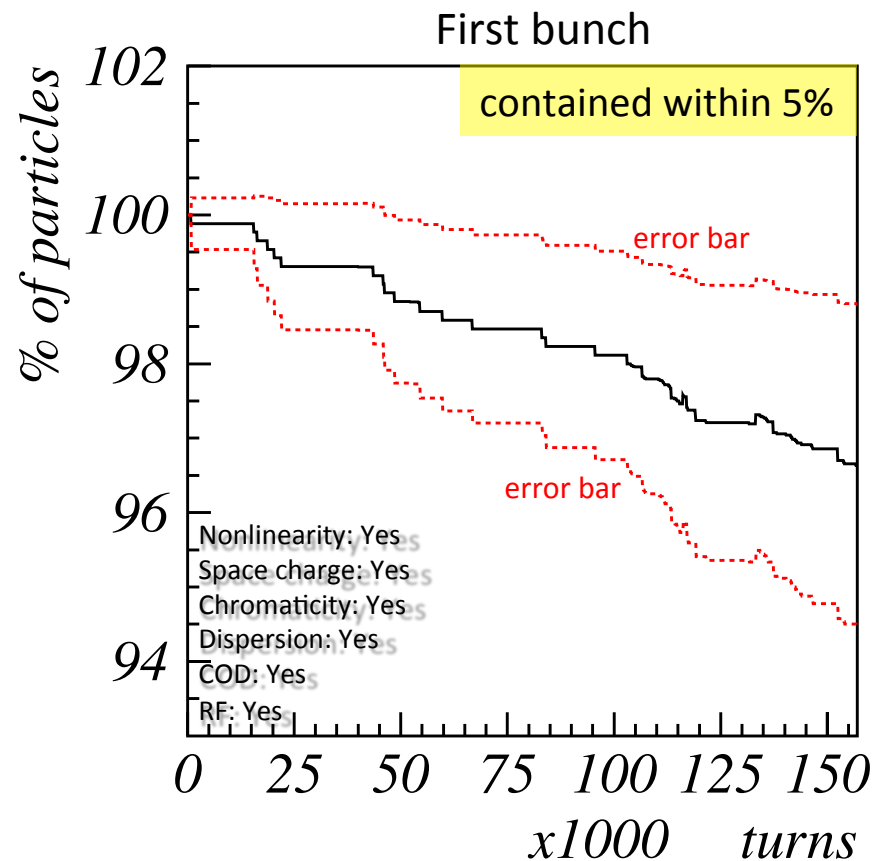


# Beam loss prediction

Compensated

Standard seed

Un-Compensated





# SUMMARY

## For the “standard error seed”

Elimination of 3<sup>rd</sup> order components cut beam loss to ~3% (academic example II)

Successful implementation of a compensation strategy for removing  $Q_x + 2Q_y = 56$  without exciting other resonances

Multi-particle simulations confirm that beam loss are cut to 2.5% +/- 2%  
No periodic resonance crossing can happen without a resonance to be crossed ;-)

**Note that  $2Q_x + 2Q_y = 56$  does not give any problem!! :**  
**Quite consistent with present understanding of periodic resonance crossing...**

**These results are theoretically valid for the standard error seed:  
what happen with the other seeds ?**



# ROBUSTNESS OF THE CORRECTION SCHEME

# Robustness of the correction scheme: first analysis

We corrected the resonance  $Q_x + 2 Q_y = 56$  for the “standard error seed” (seed #3)

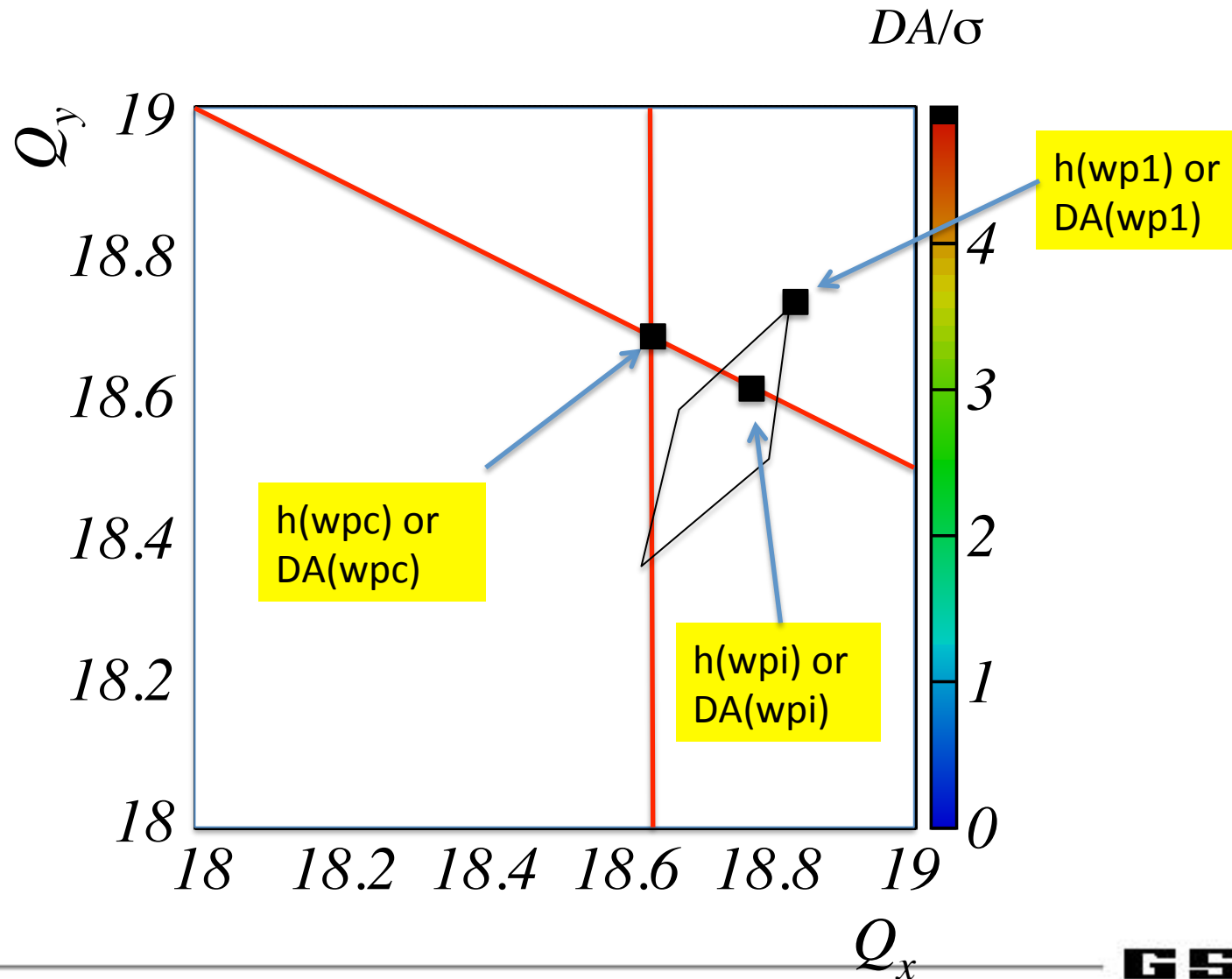
**What happen with the other 29 seeds ?**

Can we make a compensation without reducing too much DA ?

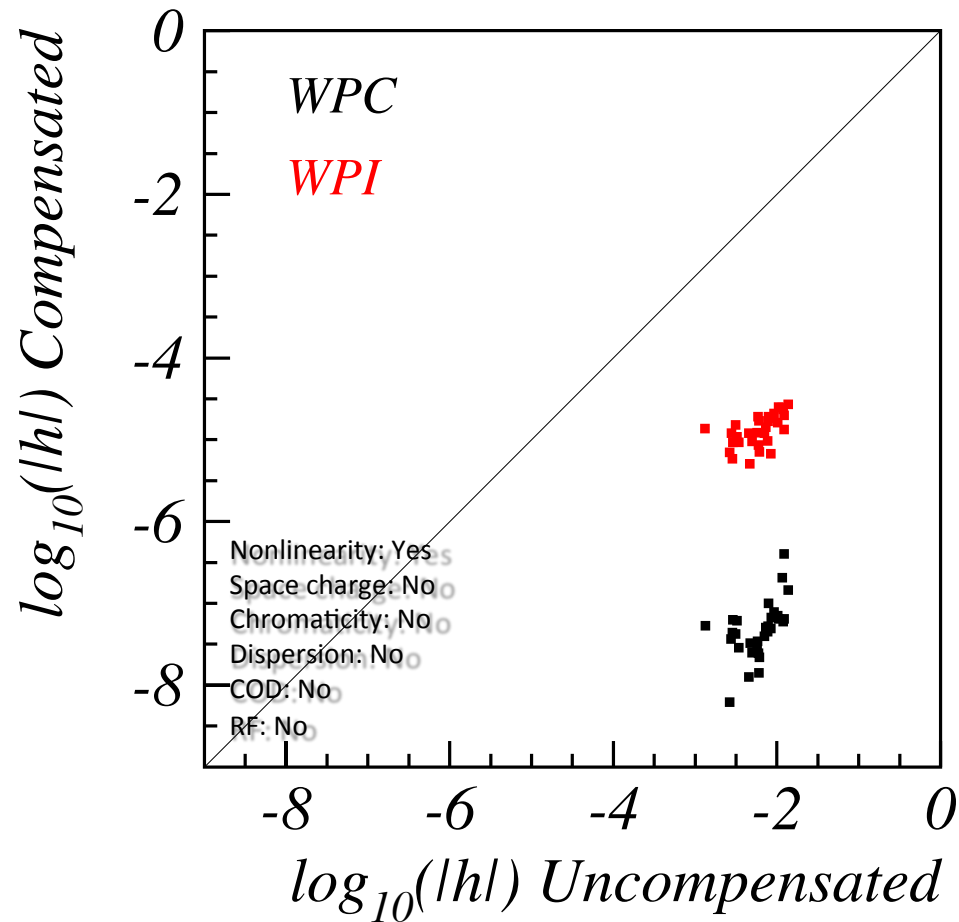
## New Issues

- 1) Does space charge affect the resonance compensation scheme?
- 2) At what level the compensation has to be carried out ?

# Definitions of the Compensation Indicators



# Statistic analysis with driving terms

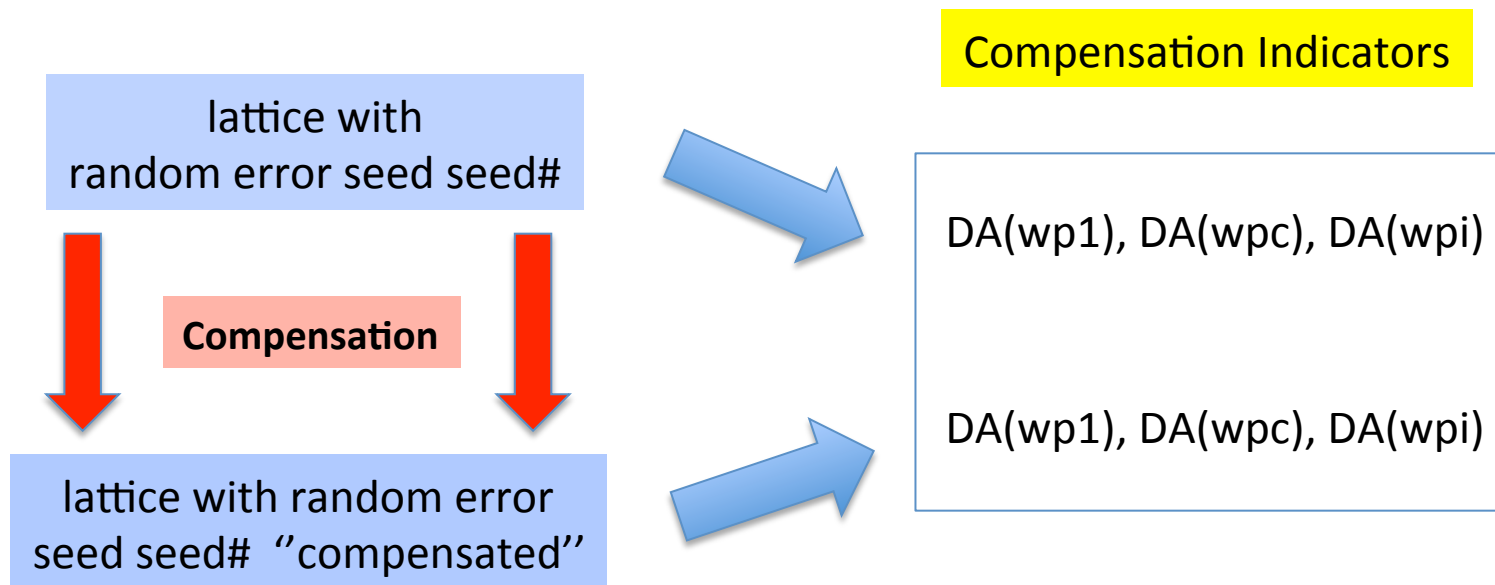


$h(wpc)$  is reduced  $\sim 5$  orders  
 $h(wpi)$  is reduced of  $\sim 3$  orders

Apparently good

# Statistic analysis with beam dynamics based Compensation Indicators

For each of the 30 seeds we compute the compensation indicators with and without compensation





# Statistical results

## Compensation indicators for the “standard error seed”

	DA(wp1) / $\sigma$	DA(wpc) / $\sigma$	DA(wpi) / $\sigma$	$b_1$ [m <sup>-3</sup> ]	$b_2$ [m <sup>-3</sup> ]	$b_3$ [m <sup>-3</sup> ]	$b_4$ [m <sup>-3</sup> ]
uncompensated	4.76	2.93	3.64	0	0	0	0
compensated	4.68	3.96	4.66	-0.05	-0.025	-0.0307	-0.0214

## Statistical analysis of the Compensation Indicators

	DA(wp1) / $\sigma$	DA(wpc) / $\sigma$	DA(wpi) / $\sigma$	$b_1$ [m <sup>-3</sup> ]	$b_2$ [m <sup>-3</sup> ]	$b_3$ [m <sup>-3</sup> ]	$b_4$ [m <sup>-3</sup> ]
uncompensated	4.64 +/- 0.10	3.18 +/- 0.45	4.03 +/- 0.30	0	0	0	0
compensated	4.64 +/- 0.09	3.94 +/- 0.23	4.39 +/- 0.14	0 +/- 0.03	0 +/- 0.03	0 +/- 0.02	0 +/- 0.02

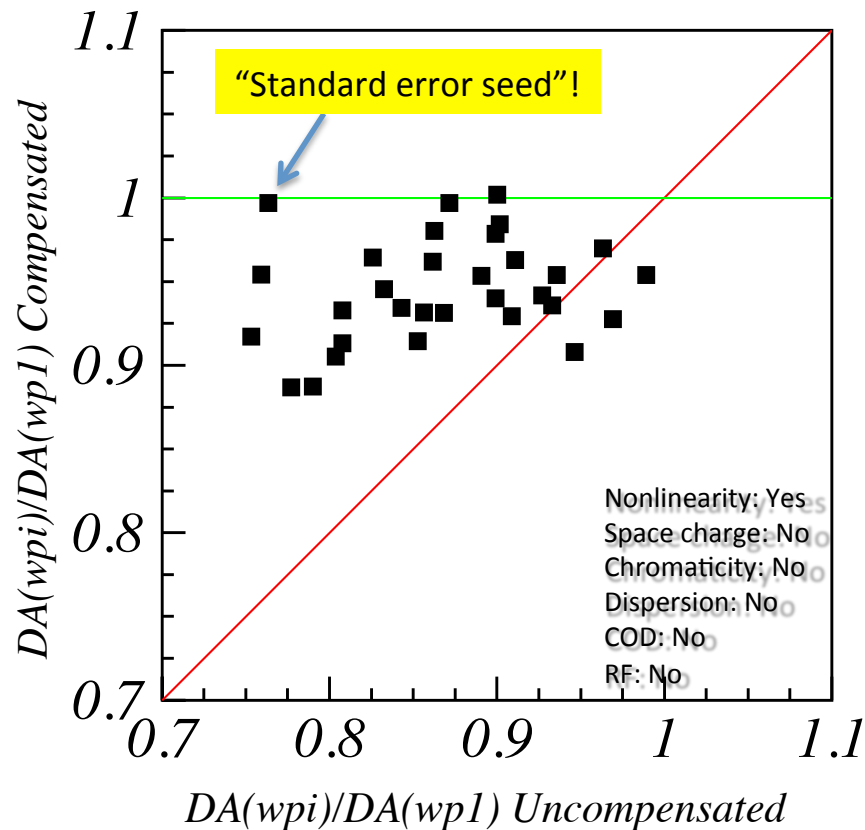
(Notation: average +/- standard deviation)

maximum effect on chromaticity  $\rightarrow \left| \frac{\partial Q_{x/y}}{\partial(\delta p/p)} \right| < 0.08$

# Existence of Residual Resonances

From the statistic we find that  $DA(wp1)$  is not affected by the correction scheme

We take  $DA = 4.7/\sigma$  as a reference value



For most cases there exists a residual resonance after compensation



The effect of the residual resonance on beam survival is not tested yet...

# SUMMARY

The method of controlling of  $Q_x + 2Q_y = 56$  on the cancellation working point reduces the driving terms of a factor larger than 100

**BUT**

Verification with beam dynamics shows that some residual resonance at WPI is still found



Multiparticle tracking should be carried out for other seeds to confirm the dependence (or absence) of beam loss performance from residual resonances

-> Development of further more complex schemes of resonance control

**Are we sure the effect of space charge does not affect the resonance compensation scheme ?**



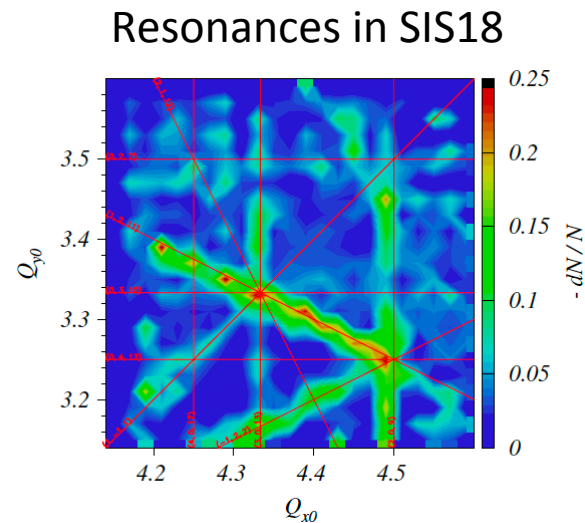
# **NEXT STEP EXPERIMENTAL VERIFICATION ON SIS18**

# Relevant issues for experiments

It becomes then necessary to develop a measurement strategy of nonlinear error

- 1) Measurement in magnets
- 2) Beam Based Measurements

**SIS18 becomes a “test accelerator” for the high intensity beam dynamics issues of SIS100**



Reconstruction of sextupolar components  
in SIS18 with the nonlinear tune response  
matrix method

Simultaneous 2 BPM acquisition

Comparing with magnet measured data

# Experimental verification in SIS18

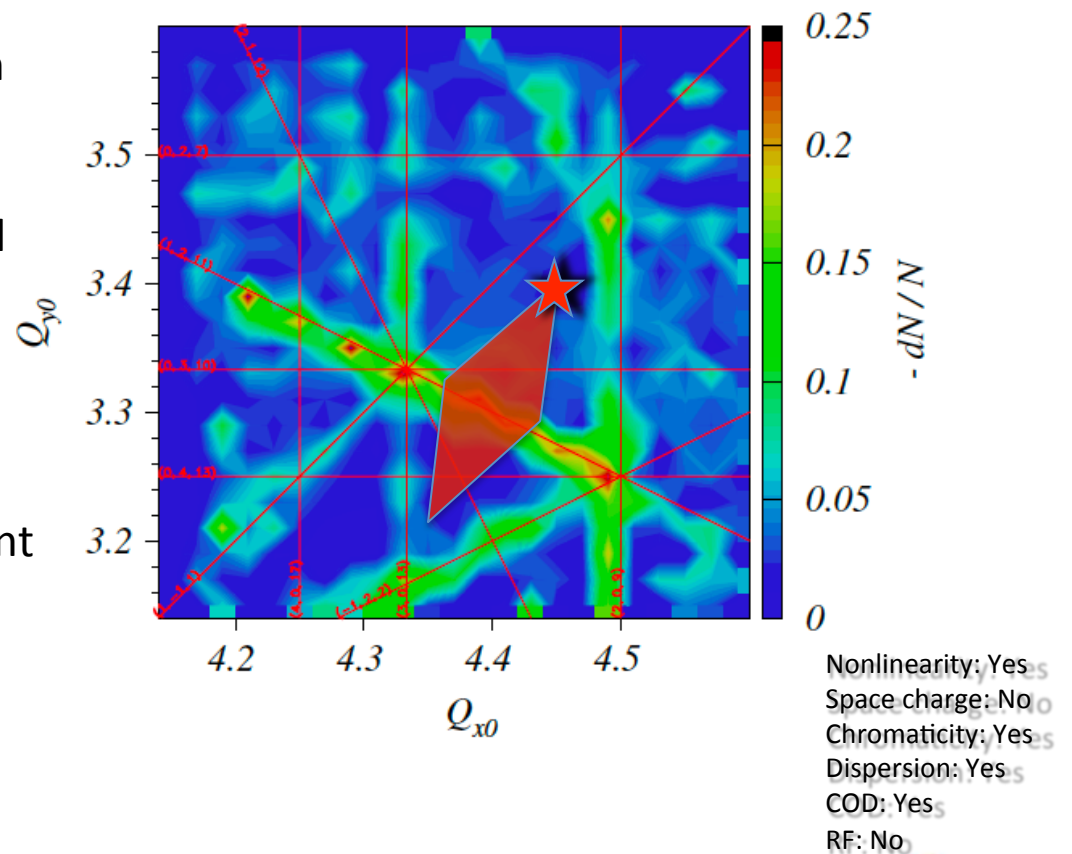
Test on SIS18 if the compensation scheme of a 3<sup>rd</sup> order resonance

$$Q_x + 2 Q_y = 11$$

works for a space charge bunched beam



- 1) Equivalent to the S317 experiment
- 2) Part of the SIS18 upgrade 2 FAIR





# Conclusion

- 1) Space charge incoherent effects are responsible for beam loss;
- 2) A dedicated measurement campaign gave us confidence that we understand the main ingredients of the space charge and resonance driven beam loss;
- 3) In order to control beam loss in a high intensity bunched beam we have to:
  - 1) Optimize the location of the working point;
  - 2) Control of the relevant resonances;
  - 3) Flatten longitudinal bunch distribution;
- 4) We have implemented for moderate error seed the compensation of the resonance  $Q_x + 2 Q_y = 56$  leaving the other resonances unchanged:  
**We find a reduction of the beam loss of a factor 10 on the first injected bunch**  
**Therefore @5E11 beam loss ~5% to be doubled to 10% (factor 2 from benchmarking)**

**Over the full cycle @5E11 after correction of  $Q_x + 2 Q_y = 56$  beam loss expected of ~5% for the “standard error seed”**

# Conclusion

- 5) **There is no prove that we are able to compensate any error seed induced resonance**: further multi-particle simulations are necessary to clarify which level of residual resonance is allowed;
- 6) Development of more efficient compensation schemes;
- 7) **It is mandatory to perform an experimental campaign in SIS18 for testing these findings.**

## Final Remarks

The simulations here presented are in some case unfinished because of several computer crash in the central system: GSI needs to power more the computer center and renew the PROCESSOR-PARK

GSI needs to form and keep the competences apt to face this class of problems for the time SIS100 will be constructed



# Optics at the location of the correction system

Corrector elements: 12 group of correctors each formed by  
1 quadrupole, 1 sextupole, 1 octupole

## Optics at the position of the corrector sextupoles for the “cancellation WP”

Nele	Label	Position	$\beta_x$	$\alpha_x$	$\psi_x/(2\pi)$	$D_x$	$D'_x$	$\beta_y$	$\alpha_y$	$\psi_y/(2\pi)$
1	corr_oct1	0	5.89921	0.07827	0	0.02449	-0.00179	17.1682	-1.39403	0
535	corr_oct2	56.6	17.78347	1.42584	0.96545	0.04476	-0.0039	5.84209	-0.03965	0.96661
2494	corr_oct3	180.6	5.89921	0.07827	3.11111	0.02449	-0.00179	17.1682	-1.39403	3.11111
3028	corr_oct4	237.2	17.78346	1.42584	4.07656	0.04476	-0.0039	5.84209	-0.03965	4.07772
4987	corr_oct5	361.2	5.89921	0.07827	6.22222	0.02449	-0.00179	17.1682	-1.39403	6.22222
5513	corr_oct6	417.8	17.78347	1.42584	7.18767	0.04476	-0.0039	5.84209	-0.03965	7.18883
7472	corr_oct7	541.8	5.89921	0.07827	9.33333	0.02449	-0.00179	17.1682	-1.39403	9.33333
7998	corr_oct8	598.4	17.78347	1.42584	10.29878	0.04476	-0.0039	5.84209	-0.03965	10.29994
9957	corr_oct9	722.4	5.89921	0.07827	12.44444	0.02449	-0.00179	17.1682	-1.39403	12.44444
10483	corr_oct10	779.0	17.78347	1.42584	13.40989	0.04476	-0.0039	5.84209	-0.03965	13.41105
12442	corr_oct11	903.0	5.89921	0.07827	15.55555	0.02449	-0.00179	17.1682	-1.39403	15.55556
12986	corr_oct12	959.6	17.78347	1.42584	16.521	0.04476	-0.0039	5.84209	-0.03965	16.52216

We split the 12 sextupoles  
into 2 families

$$K_{2,1}^1, K_{2,2}^1, K_{2,3}^1 \quad K_{2,4}^1, K_{2,5}^1, K_{2,6}^1 \quad \rightarrow \beta_x = 17.7 \text{ m}$$

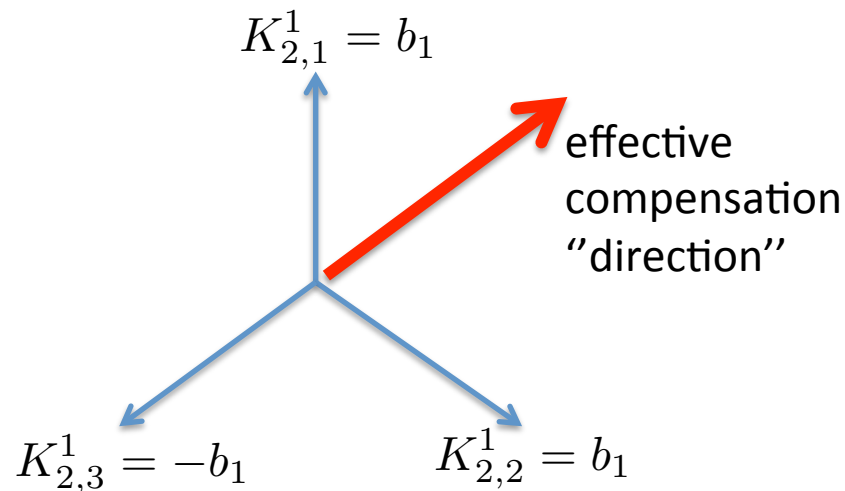
$$K_{2,1}^2, K_{2,2}^2, K_{2,3}^2 \quad K_{2,4}^2, K_{2,5}^2, K_{2,6}^2 \quad \rightarrow \beta_x = 5.8 \text{ m}$$

# Assigning the strength in each sub-family

**Minimum DA disturbance criteria:  
we require to keep the strength of the sextupoles as low as possible**

Optics considerations:

Subfamily  $K_{2,1}^1, K_{2,2}^1, K_{2,3}^1$   $\longrightarrow$  At WPC each sextupole has  $\Delta\theta = 120^\circ +$  a multiple of  $360^\circ$  from the next of the same sub-family



With this configuration the sub-family

$$K_{2,1}^1, K_{2,2}^1, K_{2,3}^1$$

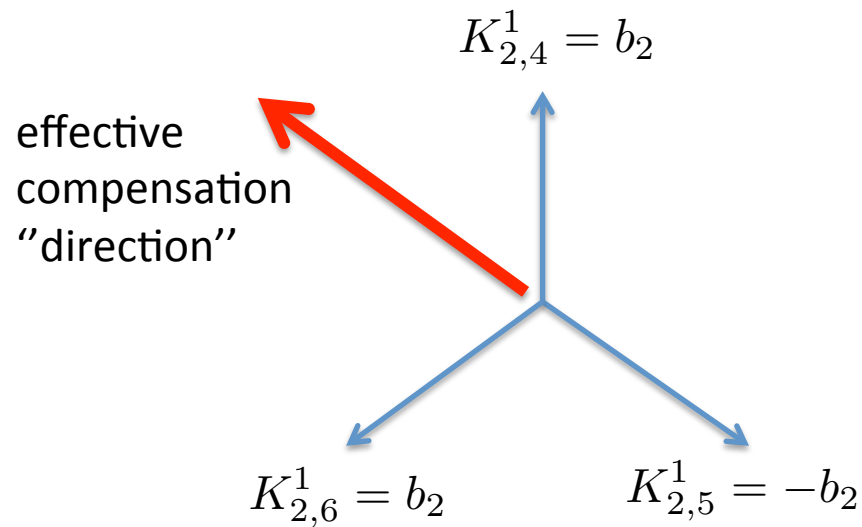
creates a driving term

$$\propto b_1 e^{i\pi/6}$$

The 3 sextupoles creates an effective strength  $\propto 2b_1$

# 2<sup>nd</sup> sub-family

Subfamily  $K_{2,4}^1, K_{2,5}^1, K_{2,6}^1$   $\rightarrow$  At WPC each sextupoles is  $\Delta\theta = 120^\circ +$  a multiple of  $360^\circ$  form the next



With this configuration the sub-family

$$K_{2,4}^1, K_{2,5}^1, K_{2,6}^1$$

creates a driving term

$$\propto b_1 e^{i\pi 5/6}$$

Therefore  $K_{2,1}^1, K_{2,2}^1, K_{2,3}^1$  and  $K_{2,4}^1, K_{2,5}^1, K_{2,6}^1$  creates two independent direction in the complex plane  $120^\circ$  degree apart

The same strategy is applied to the 2 sub-families  $K_{2,1}^2, K_{2,2}^2, K_{2,3}^2$   $K_{2,4}^2, K_{2,5}^2, K_{2,6}^2$



# Definition of sub-families

The simultaneous compensation of 2 resonances require 4 “knobs”

We divide each sub-family into 2 sub-families

Nele	Name strength	Name object
1	$K_{2,1}^2$	corr_oct1
535	$K_{2,1}^1$	corr_oct2
2494	$K_{2,2}^2$	corr_oct3
3028	$K_{2,2}^1$	corr_oct4
4987	$K_{2,3}^2$	corr_oct5
5513	$K_{2,3}^1$	corr_oct6
7472	$K_{2,4}^2$	corr_oct7
7998	$K_{2,4}^1$	corr_oct8
9957	$K_{2,5}^2$	corr_oct9
10483	$K_{2,5}^1$	corr_oct10
12442	$K_{2,6}^2$	corr_oct11
12986	$K_{2,6}^1$	corr_oct12

$$\beta_{x, \max} = 17.7 \text{ m}$$

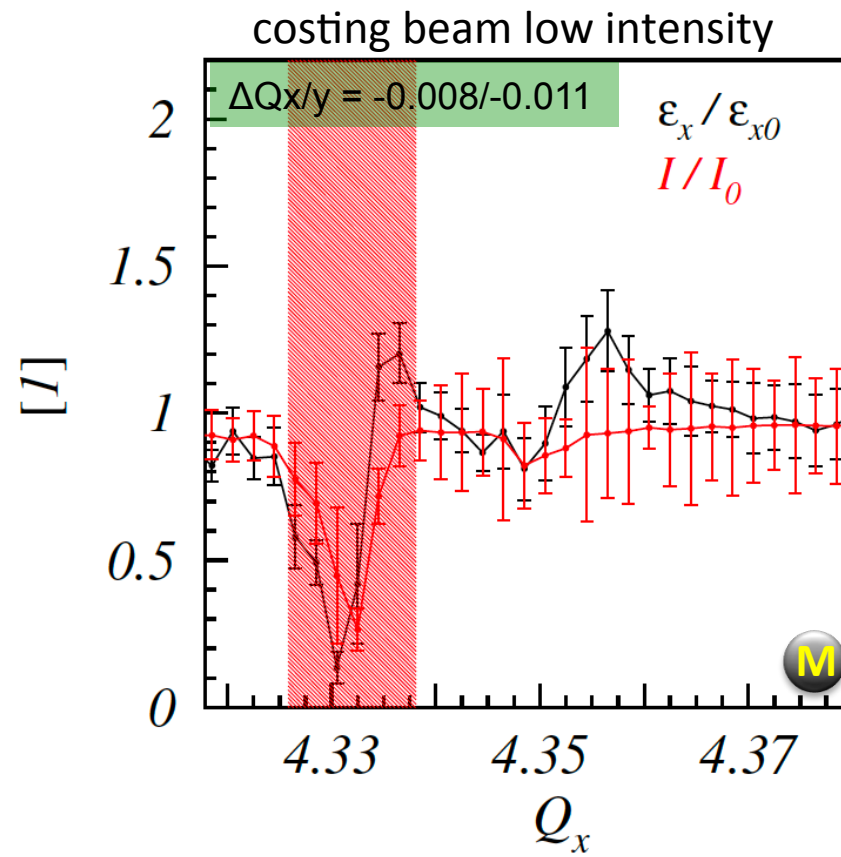
$$K_{2,1}^1, K_{2,2}^1, K_{2,3}^1 \quad K_{2,4}^1, K_{2,5}^1, K_{2,6}^1$$

$$\beta_{x, \min} = 5.8 \text{ m}$$

$$K_{2,1}^2, K_{2,2}^2, K_{2,3}^2 \quad K_{2,4}^2, K_{2,5}^2, K_{2,6}^2$$

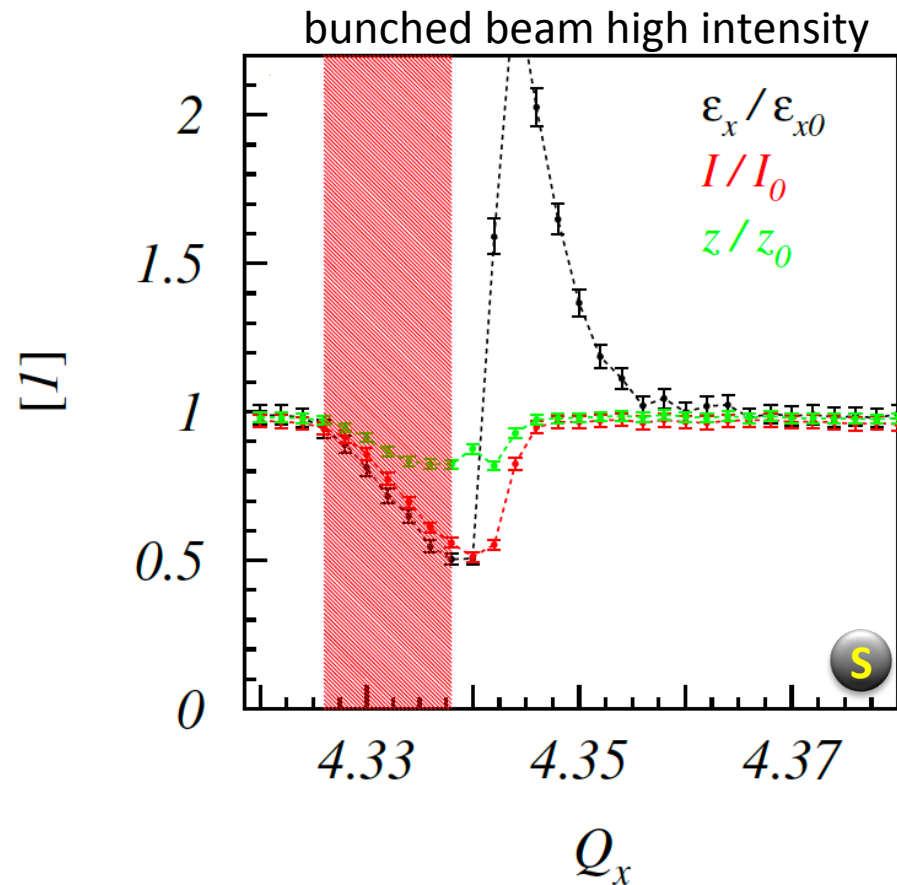
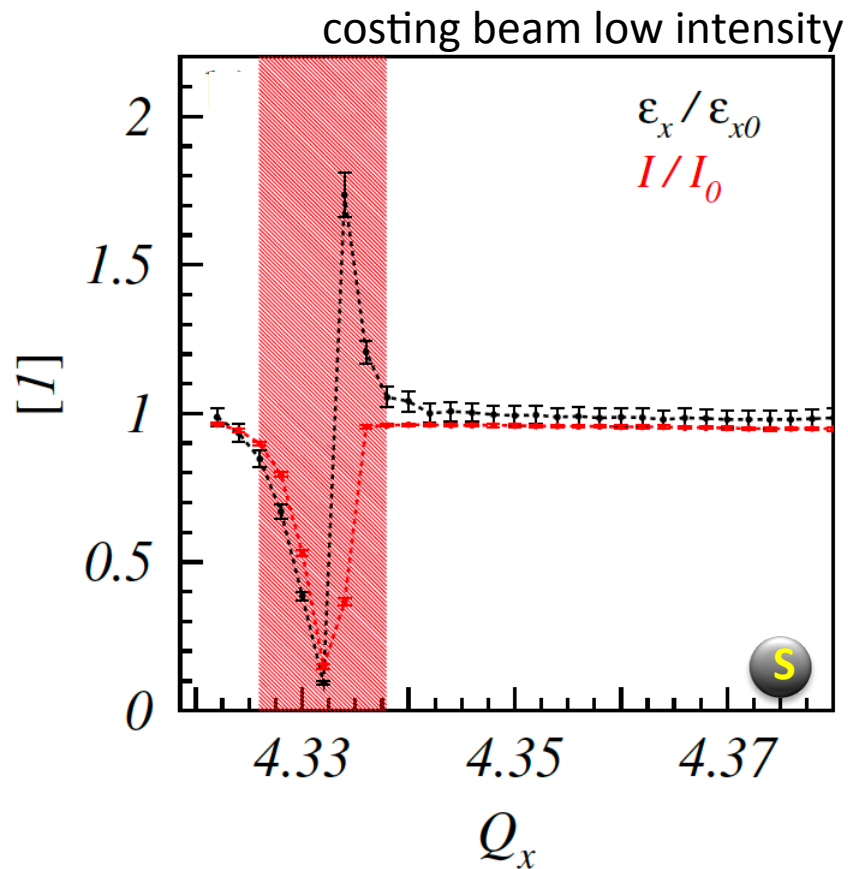
Strategy: each sub-family provides a degree of freedom in the complex plane

Optimal requirement: each family is a combination of elements which provides a 90 degree phase from the next sub-family



# Simulation benchmarking

Weak modeling of the SIS18 nonlinear dynamics close 3<sup>rd</sup> order resonance



# SIS100 multipoles

DIPOLE

```

===== the dipole model 25/6/2010 =====
|SIS100_Dipole_CSLD8b
| "Rogovsky_I1_1319kA_Cntr_Bpho_Tm_10.17_CO_xy_p0.0_p0.0_mm"
| "data_hdf/SIS100_Dipole_CSLD_Harmonics_20100609.h5:
| /Dipole/D3/Curved/CSLD8b/Rogovsky_Profile/"
MD+0 MULTIPOLE -4.7163389758317062E-03 -1.0547373696328898E-11 0
MD+1 MULTIPOLE 3.0785055973603015E-05 -5.8053823331158389E-10 1
MD+2 MULTIPOLE -2.6366697311469640E-02 -3.4266536267695576E-08 2
MD+3 MULTIPOLE 7.3195053029524795E-02 -2.4365230674135484E-06 3
MD+4 MULTIPOLE -1.2439243085067312E+02 3.8357509219972509E-05 4
MD+5 MULTIPOLE 1.5378080000548240E+02 3.0914907235399965E-02 5
MD+6 MULTIPOLE -8.6451329022645557E+04 -1.8565663052472367E+01 6
MD+7 MULTIPOLE -3.0816832178552798E+05 -4.5835022334820633E+03 7
MD+8 MULTIPOLE -1.4944190003612607E+09 1.3534633120010719E+06 8
MD+9 MULTIPOLE -2.8271535894108959E+10 3.8163902568321079E+08 9
MD+10 MULTIPOLE 1.1525179718432939E+14 -9.2536963799966492E+10 10
MD+11 MULTIPOLE 1.2805669617742790E+15 -2.7857736036314035E+13 11
MD+12 MULTIPOLE -2.1999264938605724E+18 4.4905049474379860E+15 12
MD+13 MULTIPOLE -5.0851929146109133E+19 1.4538233978336215E+18 13
MD+14 MULTIPOLE 2.0686832547682220E+22 -1.2575953096211676E+20 14
MD+15 MULTIPOLE 7.3450854860770844E+23 -4.3003206361307635E+22 15

|SIS100_Dipole_CSLD8b
| "Rogovsky_I1_1319kA_Cntr_Bpho_Tm_10.17_CO_xy_p0.0_p0.0_mm"
| "data_hdf/SIS100_Dipole_CSLD_Harmonics_20100609.h5:
| /Dipole/D3/Curved/CSLD8b/Rogovsky_Profile/"
MDC0 MULTIPOLE -4.8321734468527902E-02 -8.0460622403658862E-11 0
MDC1 MULTIPOLE 1.3222876973075998E-06 -4.4286349322627113E-09 1
MDC2 MULTIPOLE -1.5411882617349000E-02 -2.6132592908204184E-07 2
MDC3 MULTIPOLE -3.7034493848285333E-03 -1.8537012098860845E-05 3
MDC4 MULTIPOLE 4.5506880778861124E+01 2.9261019441204273E+04 4
MDC5 MULTIPOLE -6.2559995183645212E+00 2.3583431753596007E+01 5
MDC6 MULTIPOLE 7.3051033143311797E+04 -1.4162812922709435E+02 6
MDC7 MULTIPOLE -1.4288951062831108E+05 -3.4965239042733432E+04 7
MDC8 MULTIPOLE 2.2831975374350262E+09 1.0324892588690210E+07 8
MDC9 MULTIPOLE 1.0564506501167362E+10 2.9113326625983242E+09 9
MDC10 MULTIPOLE -1.6359949140068581E+14 -7.0591807199292908E+11 10
MDC11 MULTIPOLE -6.9868818985378656E+13 -2.1251269228490359E+14 11
MDC12 MULTIPOLE 2.5207268897163274E+18 3.4255809404212480E+16 12
MDC13 MULTIPOLE 1.6101150642536155E+19 1.1090489334002389E+19 13
MDC14 MULTIPOLE -2.266762204271218E+23 -9.5935636945850047E+20 14
MDC15 MULTIPOLE -8.9215833271142267E+22 -3.2804988706914617E+23 15

|SIS100_Dipole_CSLD8b
| "Rogovsky_I1_1319kA_Exit_Bpho_Tm_10.17_CO_xy_p0.0_p0.0_mm"
| "data_hdf/SIS100_Dipole_CSLD_Harmonics_20100609.h5:
| /Dipole/D3/Curved/CSLD8b/Rogovsky_Profile/"
MD-0 MULTIPOLE -4.7138405749040302E-03 -1.2991132072721643E-11 0
MD-1 MULTIPOLE 8.2298425078906093E-05 -7.1504519323945776E-10 1
MD-2 MULTIPOLE -2.5429816100754250E-02 -4.2193554515923325E-08 2
MD-3 MULTIPOLE 1.8570007483834530E-01 -3.0010497284566724E-06 3
MD-4 MULTIPOLE -1.1505080048691593E+02 4.7244696421450073E-05 4
MD-5 MULTIPOLE 4.9635167510791450E+02 3.8077691609973333E-02 5
MD-6 MULTIPOLE -4.1063310345945916E+04 -2.2867207296236053E+01 6
MD-7 MULTIPOLE 7.4381818310866482E+05 -5.6454701035899407E+03 7
MD-8 MULTIPOLE -2.36945727786783257E+09 1.6670520215659430E+06 8
MD-9 MULTIPOLE -3.4309559893775809E+08 4.7006232355151188E+08 9
MD-10 MULTIPOLE 1.4223443489744228E+14 -1.1397718076645877E+11 10
MD-11 MULTIPOLE -1.1221740140895050E+15 -3.4312193588405953E+13 11
MD-12 MULTIPOLE -2.9902753171154821E+18 5.5309259468893420E+15 12
MD-13 MULTIPOLE 5.8658711948882985E+19 1.7906648912458665E+18 13
MD-14 MULTIPOLE 2.8992131756741854E+22 -1.5489720220994719E+20 14
MD-15 MULTIPOLE -2.9914139190013502E+24 -5.2966771587902469E+22 15

```

Entrance

Body

Exit

## QUADRUPOLE

```

===== model of quadrupole 25/6/2010 =====
|SIS100_Quadrupole6Turn
| "Quadr6TurnsV1_I1_460kA_Cntr_Bpho_Tm_12.23_CO_xy_p0.0_p0.0_mm"
| "data_hdf/SIS100_Quadrupole6Turn_20100623.h5:
| /Quadrupole/Turns6/D3/OperaCalc/StaticCalculation/V1/"
Eqb0 MULTIPOLE -2.6789881018894428E-14 5.5045898388867806E-14 0
Eqb1 MULTIPOLE 2.1717022154679769E-01 1.9856320529300420E-12 1
Eqb2 MULTIPOLE -9.4521226576818973E-11 1.9401448718616971E-10 2
Eqb3 MULTIPOLE 3.7858283188846437E-03 1.0501181037334316E-08 3
Eqb4 MULTIPOLE 7.0414842692841817E-07 -1.4318783375984776E-06 4
Eqb5 MULTIPOLE 3.0194294633632222E+02 -2.8051263507461471E-04 5
Eqb6 MULTIPOLE -7.8478544512944073E-02 1.6019533278747095E-01 6
Eqb7 MULTIPOLE -1.8269515944715394E+06 2.5709785026550517E+01 7
Eqb8 MULTIPOLE 4.775705574752483E+03 -9.7507153716628163E+03 8
Eqb9 MULTIPOLE 1.585341717689340E+11 -1.7429770135777944E+06 9
Eqb10 MULTIPOLE -2.5512932132258266E+08 5.2083611876728094E+08 10
Eqb11 MULTIPOLE -6.9973814003639240E+15 9.9896489034391388E+10 11
Eqb12 MULTIPOLE 9.8111951662320020E+12 -2.0032780989903805E+13 12
Eqb13 MULTIPOLE 1.2725759662788647E+20 -4.1250219682152360E+15 13
Eqb14 MULTIPOLE -2.1305597834814832E+17 4.3518970770377338E+17 14
Eqb15 MULTIPOLE -8.7801330870650991E+23 9.4854103306132488E+19 15

|SIS100_Quadrupole6Turn
| "Quadr6TurnsV1_I1_460kA_End_Bpho_Tm_12.23_CO_xy_p0.0_p0.0_mm"
| "data_hdf/SIS100_Quadrupole6Turn_20100623.h5:
| /Quadrupole/Turns6/D3/OperaCalc/StaticCalculation/V1/"
Eqf0 MULTIPOLE -2.7060318826655702E-13 1.1626213256498432E-13 0
Eqf1 MULTIPOLE 3.1164889913266550E-02 3.7901786032567582E-12 1
Eqf2 MULTIPOLE -9.5477779762820312E-10 4.096926028596951E-10 2
Eqf3 MULTIPOLE -1.4490292439969379E-01 2.0044610087550655E-08 3
Eqf4 MULTIPOLE 7.1127170011828505E-06 -3.0181254972048956E-06 4
Eqf5 MULTIPOLE 3.7933624599308937E+03 -5.3544165092945964E-04 5
Eqf6 MULTIPOLE -7.9272672909384778E-01 3.379133954747612E-01 6
Eqf7 MULTIPOLE 3.2031177498768162E+07 4.9074727624193621E+01 7
Eqf8 MULTIPOLE 4.8259166343405115E+04 -2.0567353101754215E+04 8
Eqf9 MULTIPOLE -1.4378359763176462E+12 -3.3269865841288578E+06 9
Eqf10 MULTIPOLE -2.5771111689094310E+09 1.0986636546656621E+09 10
Eqf11 MULTIPOLE -2.9558496053583675E+15 1.9068195721472757E+11 11
Eqf12 MULTIPOLE 9.9104811140321641E+13 -4.2259100934876094E+13 12
Eqf13 MULTIPOLE 1.0139123133611631E+21 -7.873822857503470E+15 13
Eqf14 MULTIPOLE -2.1521204668226107E+18 9.1809992911089267E+17 14
Eqf15 MULTIPOLE -2.5358360899375195E+25 1.8105707307445312E+20 15

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Body

Entrance/Exit

V. Kapin visit Summer 2010

