

SIS100 FoS dipole: beam physics aspects

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SIS100 Beam Dynamics:
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SIS100 BEAM DYNAMICS SO FAR

Dynamic Aperture (DA), Beam Loss studies with the Computational Model Magnets (B_n, A_n):

- 1st MAC 2009: nonlinear dynamics, DA scans (talk Franchetti)
- 4th MAC 2010: beam loss simulations, slow extraction (talks Franchetti, Sorge)
- 5th MAC 2011: beam loss during ramp (talk Franchetti)

Main conclusions:

with the Computational Model Magnets and 30% random error ($\delta B_{n \text{ RMS}} = 0.3 B_n$)

- DA is generally safe ($>3\epsilon$), beam loss $\approx 5\%$
- beam loss is due to **combination** Space-Charge with Field-Errors + beam width (contrary to Nuclotron)
- resonance compensation necessary

Discussion at 10th MAC 2013:

Comparison of (B_n, A_n) for FoS Magnet vs. Computational Model is the base.

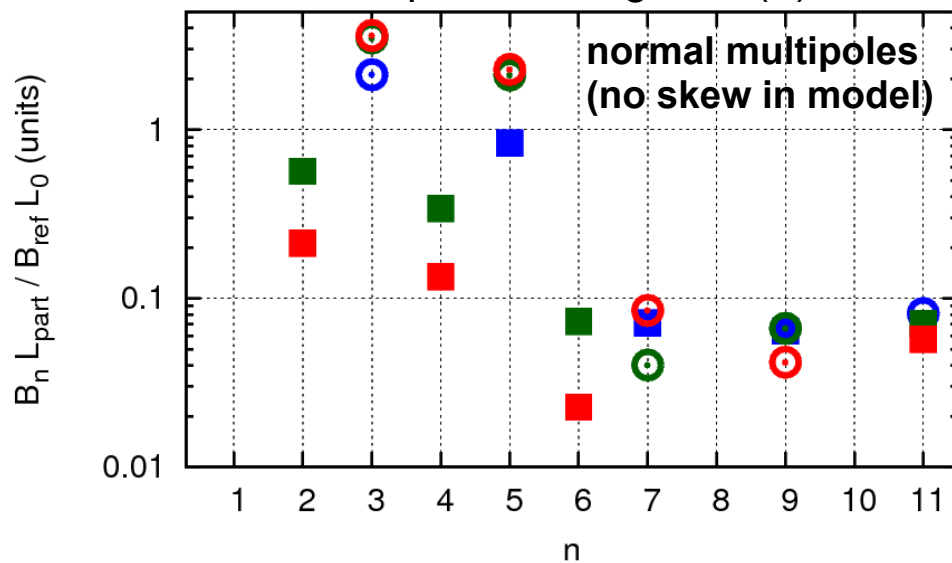
In the case of a good agreement (below $2\sigma_{\text{meas}}$), the satisfactory field quality can be concluded.

SIS100 MAGNETS: COMPUTATIONAL MODEL

Dipole Magnet (108 in SIS100)
 Computational Model Akishin et.al. 2010, Kapin et.al. 2010

Center (red), Conn-End (blue), Nonconn-End (green)

circle ○: positive (+)
 square ■: negative (-)



$B_n^{error} = B_n^{syst} + B_n^{random} = B_n + \delta B_n \times \text{Gaussian}$
 δB_n is the rms spread of the error

Our assumption so far: $\delta B_n = 0.3 B_n$:

- Is it appropriate, to relate δB_n to B_n ?
- Is the number 0.3 appropriate?

$n=1$ dipole, $n=2$ quadrupole, ...

$r_0 = 40\text{mm}$

1 unit = 10^{-4}

averaged over

$L_{center} = 2.52\text{m}$, $L_{end} = 0.4\text{m}$

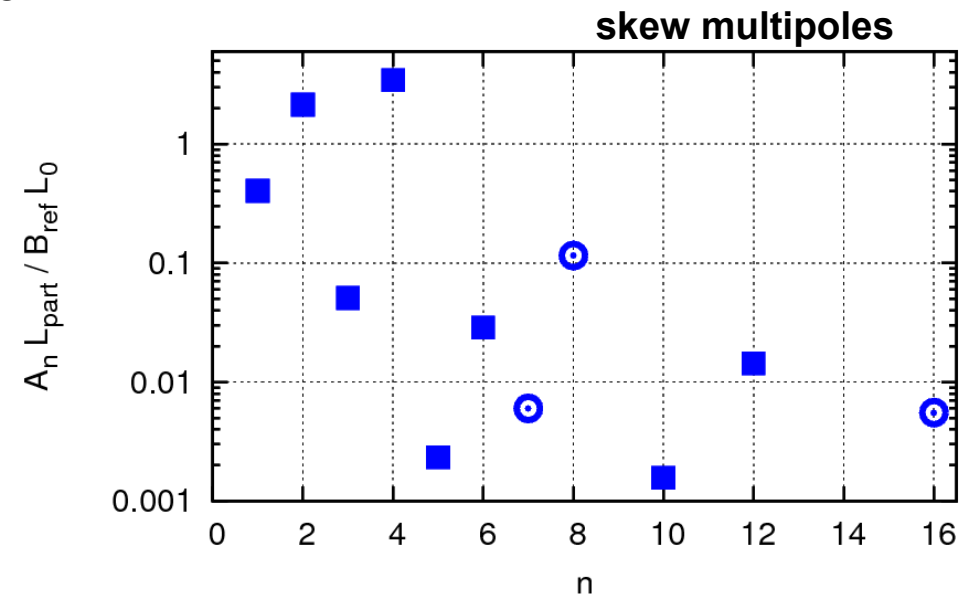
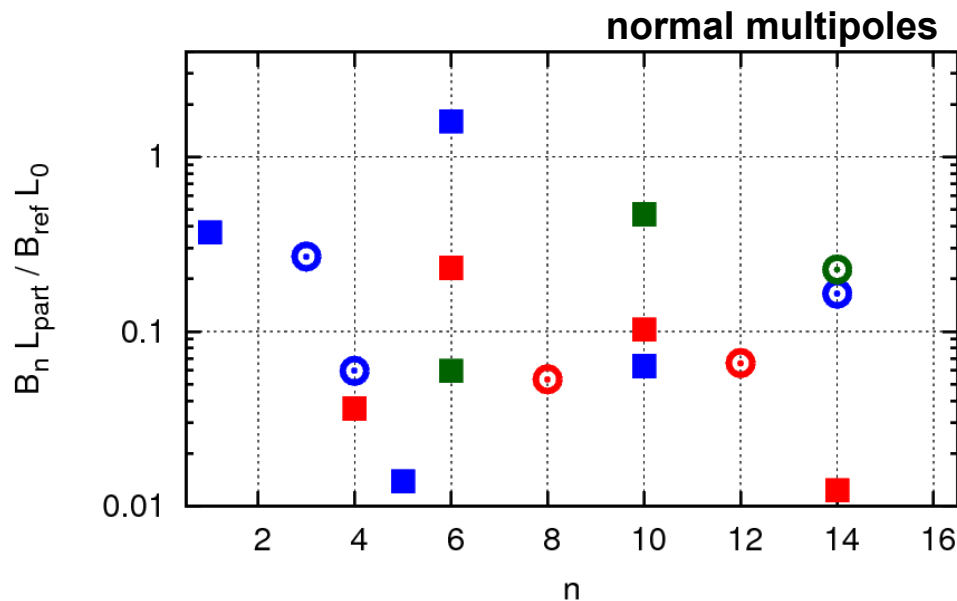
$$B_y + iB_x = \sum_{n=1} (B_n + iA_n) \left(\frac{x + iy}{r_0} \right)^{n-1}$$

SIS100 MAGNETS: COMPUTATIONAL MODEL

Quadrupole Magnet (166 in SIS100 + 2 warm)
 Computational Model Akishin et.al. 2010, Sugita 2013

Center (red), Conn-End (blue), Nonconn-End (green)

circle ○: positive (+)
 square ■: negative (-)



$n=1$ dipole, $n=2$ quadrupole, ...
 $r_0=40\text{mm}$, 1 unit = 10^{-4}

averaged over
 $L_{center}=0.96\text{m}$, $L_{end}=0.35\text{m}$

skew multipoles for the
 nonconnection-end from the
 recent simulations by K.Sugita;
 center, conn-end: no skews

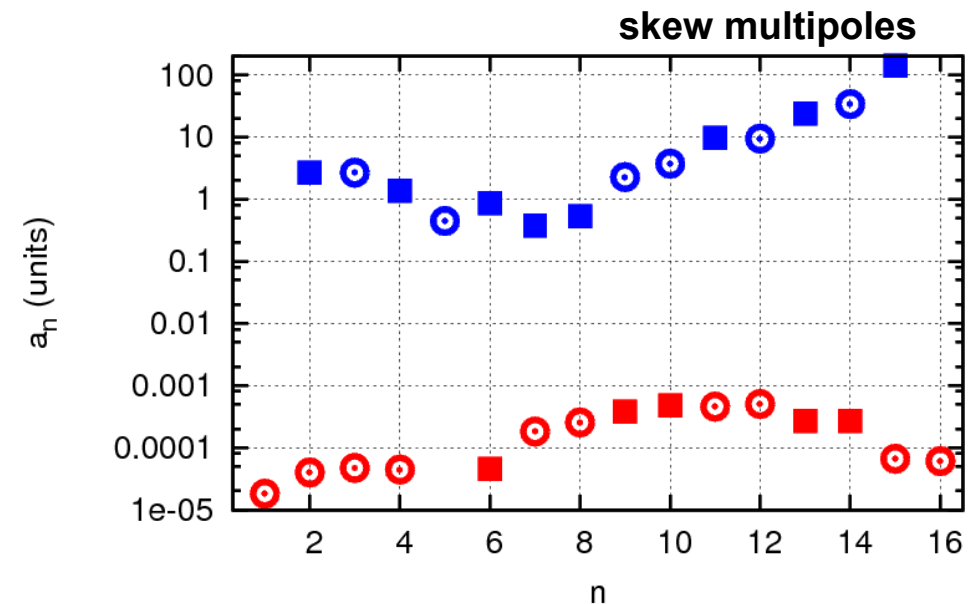
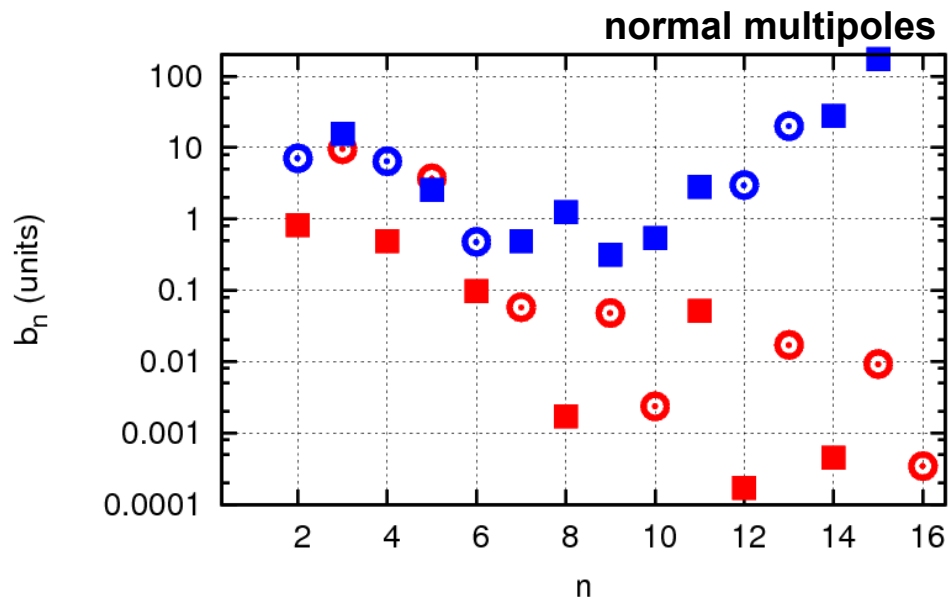
COMPARISON FOS VS COMP.MODEL

Complete Dipole Magnet $B_p=15.8\text{Tm}$

Computational Model (red), Measurements 1Coil FoS (blue)

circle \odot : positive (+)

square \blacksquare : negative (-)



$$B_y + iB_x = \sum_{n=1} (B_n + iA_n) \left(\frac{x + iy}{r_0} \right)^{n-1}$$

$n=1$ dipole, $n=2$ quadrupole,...

$r_0=40\text{mm}$

$b_n=B_n/B_1$, $a_n=A_n/B_1$

1 unit = 10^{-4}

averaged over $L_0=3.6\text{m}$

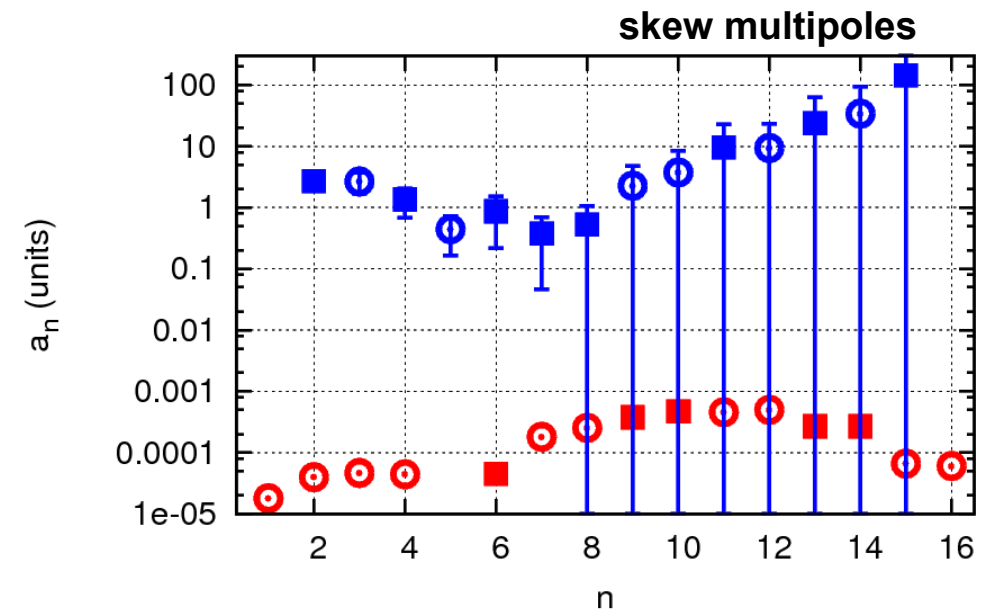
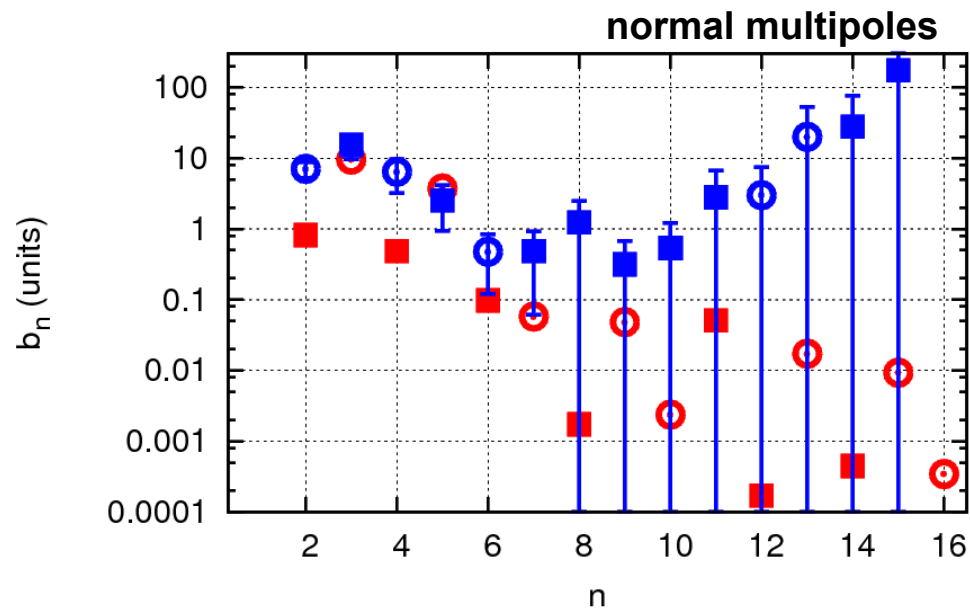
COMPARISON FOS VS COMP.MODEL

Complete Dipole Magnet $B_p=15.8\text{Tm}$

Computational Model (red), Measurements 1Coil FoS (blue) with the Error Bars

circle \circ : positive (+)

square \blacksquare : negative (-)



$n=1$ dipole, $n=2$ quadrupole, ...
 $r_0=40\text{mm}$, 1 unit = 10^{-4} , $b_n=B_n/B_1$, $a_n=A_n/B_1$

Conclusion: consider only $n \leq 7$.
 the magnet differs from the computational model.

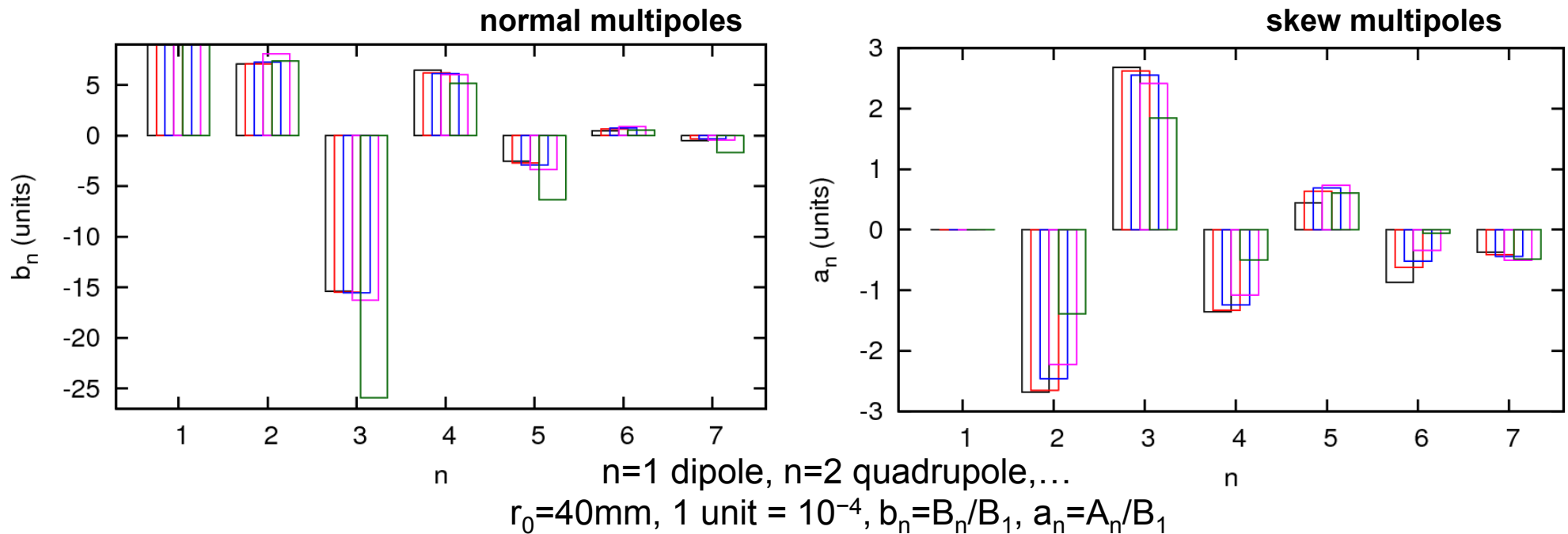
FOS MAGNET MULTIPOLES

Complete magnet: Measurements with 1 (central) coil without end-block optimization

Current (kA): 2, 4, 6, 10, 13.1

B_p (Tm): 15.8, 31.5, 47.3, 79, 103

SIS100 Operation: from $B_p=18$ Tm to $B_p=100$ Tm



Multipoles do not change significantly with the increasing current

FOS DIPOLE MAGNET MULTIPOLES

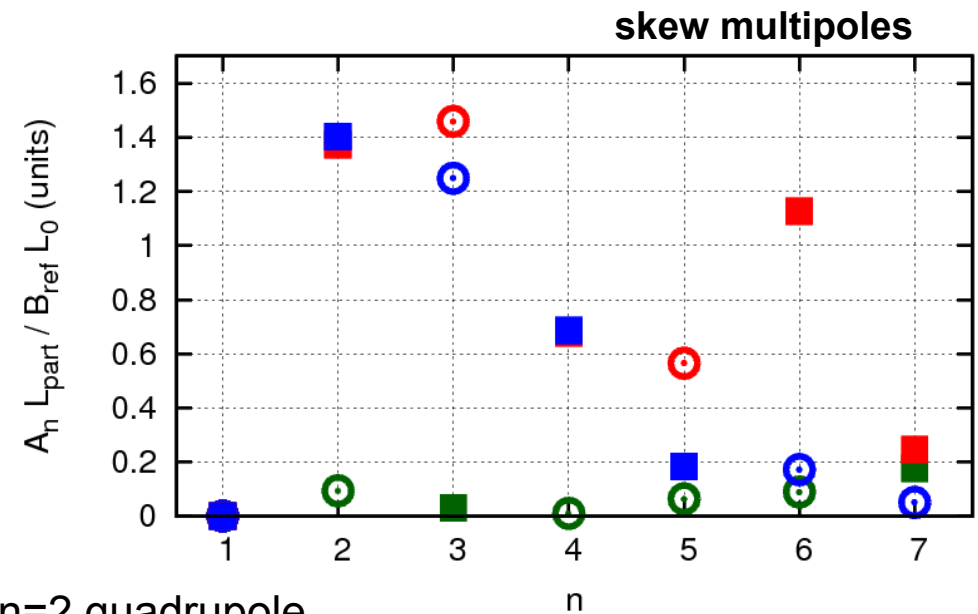
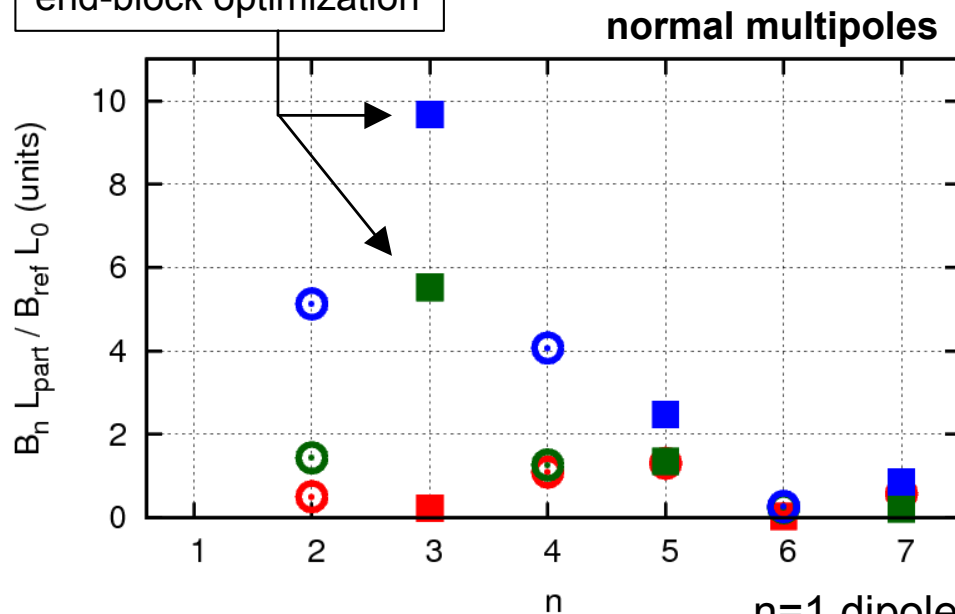
Measurements with 1 (central) coil without end-block optimization

Center (red), NonConn-End (blue), Conn-End (green)

circle ○: positive (+)

square ■: negative (-)

will be reduced by the end-block optimization



n=1 dipole, n=2 quadrupole, ...
 $r_0=40\text{mm}$, 1 unit = 10^{-4} , averaged over $L_{\text{center}}=2.4\text{m}$, $L_{\text{end}}=0.6\text{m}$

Consider only $n \leq 7$.
 Confirmed by other magnetic measurements (talk P.Schnizer)

Assumption: these are the **systematic** multipoles

FOS DIPOLE MAGNET MULTIPOLES

$$\mathbf{B}_2^{\text{error}} = \mathbf{B}_2^{\text{syst}} + \mathbf{B}_2^{\text{random}}$$

$\mathbf{B}_2^{\text{syst}}$ -Component produces **tune shift**:

$$\Delta Q_x = 18.74 - 18.84 = -0.1$$

$$\Delta Q_y = 18.81 - 18.73 = +0.08$$

Fully compensated with the Main Quadrupoles.

$\mathbf{A}_2^{\text{syst}}$ produces linear coupling

$\mathbf{B}_2^{\text{random}}$ excites 2nd order resonances

$\mathbf{A}_2^{\text{random}}$ excites 2nd order coupling resonances

$$\mathbf{B}_3^{\text{error}} = \mathbf{B}_3^{\text{syst}} + \mathbf{B}_3^{\text{random}}$$

$\mathbf{B}_3^{\text{syst}}$ produces **chromaticity shift**:

$$\Delta Q \xi_x = -34.8 - (-25.8) = -9.0 \text{ (non-optimized)}$$

$$\Delta Q \xi_y = -18.5 - (-25.7) = +7.2 \text{ (non-optimized)}$$

$$\Delta(\text{SL}_{\text{eff}})_x = -17\text{T/m}; \Delta(\text{SL}_{\text{eff}})_y = -21\text{T/m}$$

(magnet strength 175T/m, 170T/m for full ξ compensation)

$\mathbf{B}_3^{\text{random}}$ excites 3rd order resonances

$\mathbf{A}_3^{\text{random}}$ excites 3rd order coupling resonances

$$\mathbf{B}_4^{\text{error}} = \mathbf{B}_4^{\text{syst}} + \mathbf{B}_4^{\text{random}}$$

$\mathbf{B}_4^{\text{syst}}$ produces ampl.-dependent tune shift:

$$\Delta Q_x(a_{x, \text{beam}}) = 0.044$$

$$\Delta Q_y(a_{y, \text{beam}}) = 0.018$$

(12 Corrector octupoles 3 \times stronger)

$\mathbf{A}_4^{\text{syst}}$ does not produce 1st order ΔQ

$$\mathbf{B}_n^{\text{error}} = \mathbf{B}_n^{\text{syst}} + \mathbf{B}_n^{\text{random}}$$

$$\mathbf{A}_n^{\text{error}} = \mathbf{A}_n^{\text{syst}} + \mathbf{A}_n^{\text{random}}$$

$\mathbf{B}_n^{\text{random}}$ excites nth order resonances

$\mathbf{A}_n^{\text{random}}$ excites nth order coupling resonances

RESONANCES

Ions Fast Extraction

$$Q_{X0} = 18.84$$

$$Q_{Y0} = 18.73$$

The tune footprint due to space charge and chromaticity with δp

B2: normal quadrupole

A2: skew quadrupole

B3: normal sextupole

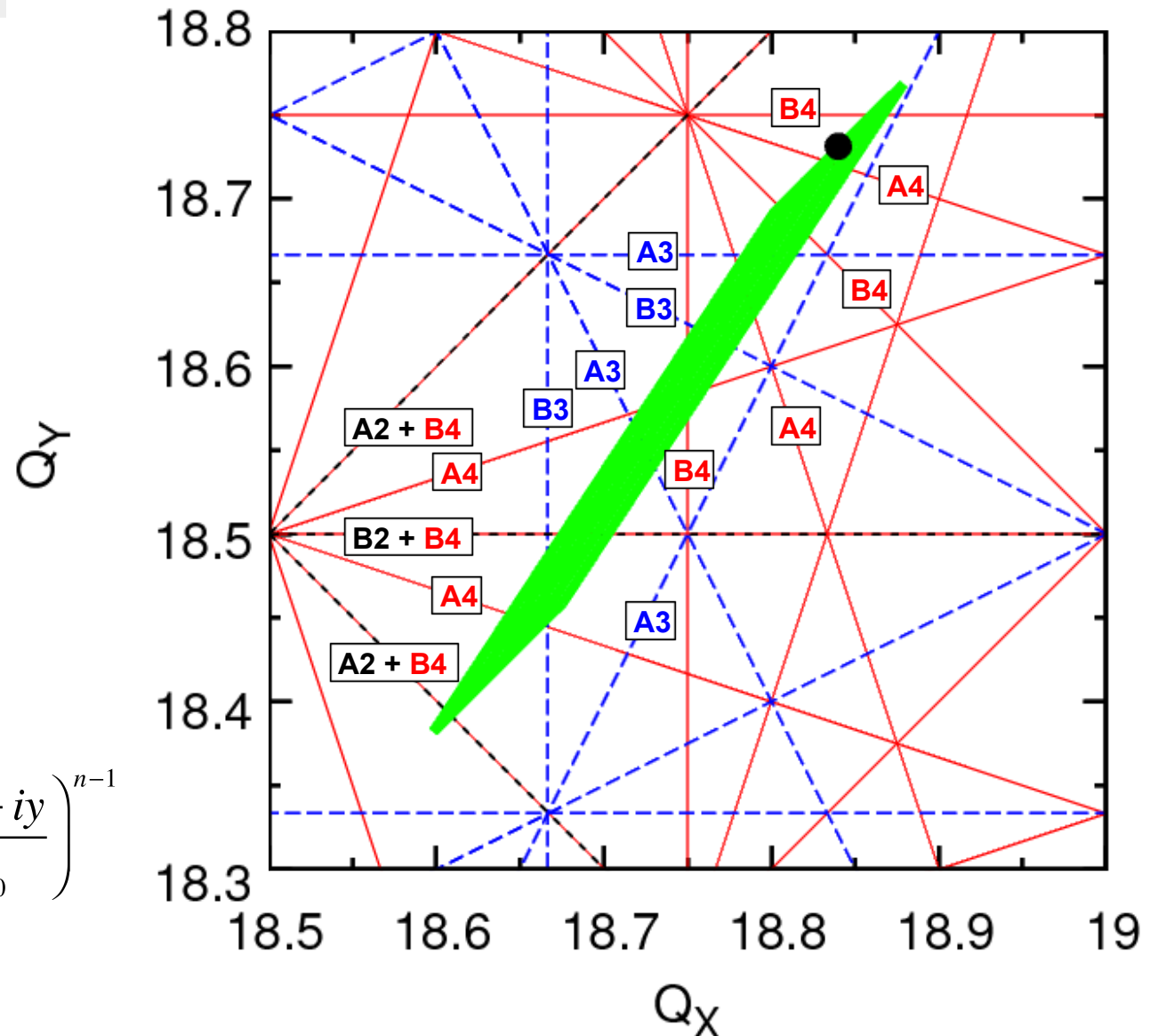
A3: skew sextupole

B4: normal octupole

A4: skew octupole

$$B_y + iB_x = \sum_{n=1} (B_n + iA_n) \left(\frac{x + iy}{r_0} \right)^{n-1}$$

\setminus coupling sum
 $/$ coupling difference



RESONANCES

Resonance Compensation
at SIS100

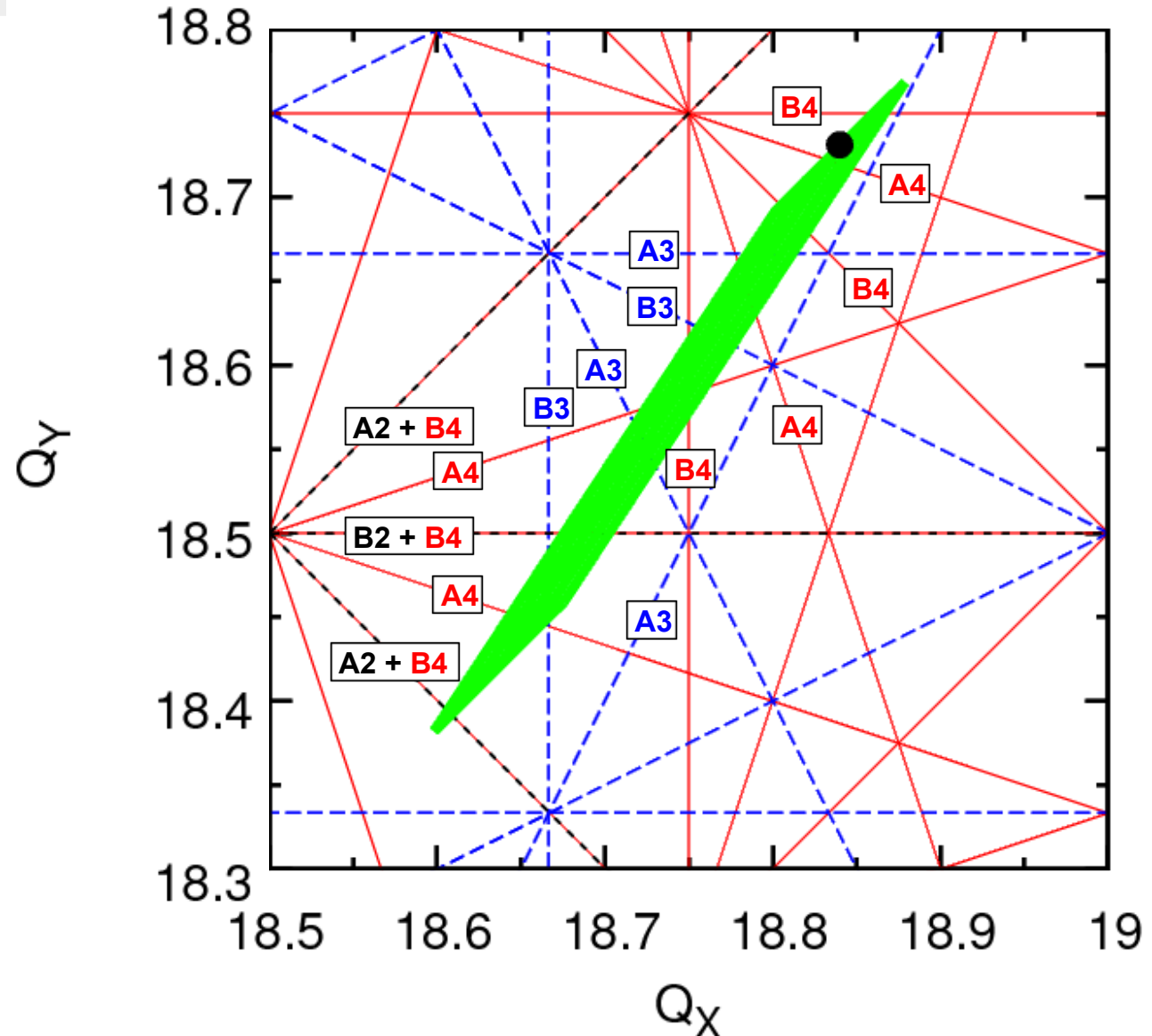
12 Corrector Quadrupoles
(**B2**) 0.75T/m, 0.75m
30× stronger than B_2^{sys} FoS

no skew Quadrupoles (**A2**)

42 ξ -Sextupoles (**B3**)
350T/m², 0.5m
176× stronger than B_3^{sys} FoS
(plus 6 Resonance Sext)

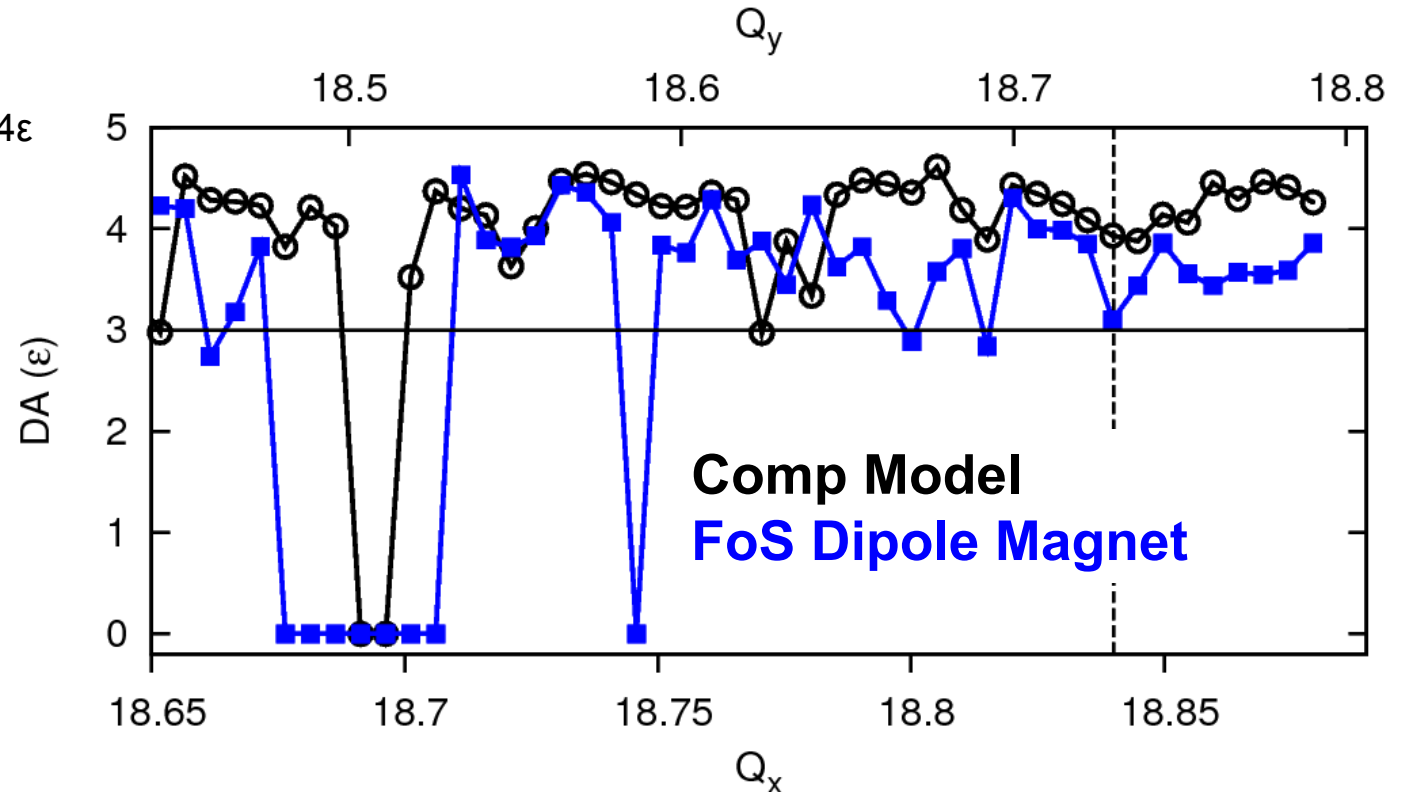
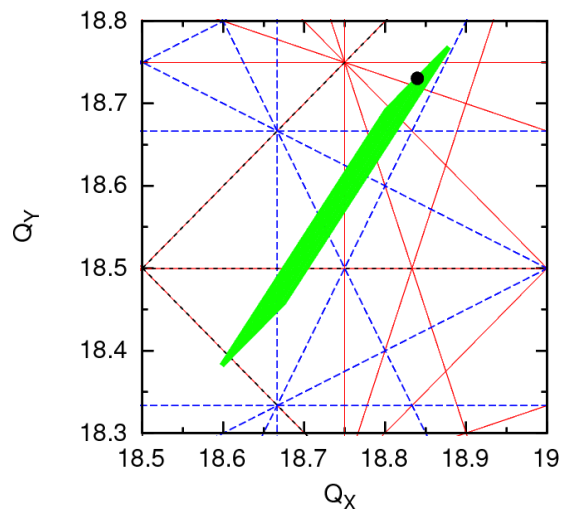
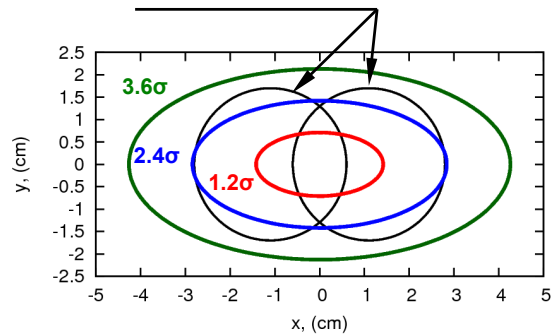
12 Corrector Skew Sext (**A3**)
50T/m², 0.75m
145× stronger than A_3^{sys} FoS

12 Corrector Octupoles (**B4**)
2000T/m³, 0.75m
25× stronger than B_4^{sys} FoS



DYNAMIC APERTURE SCANS

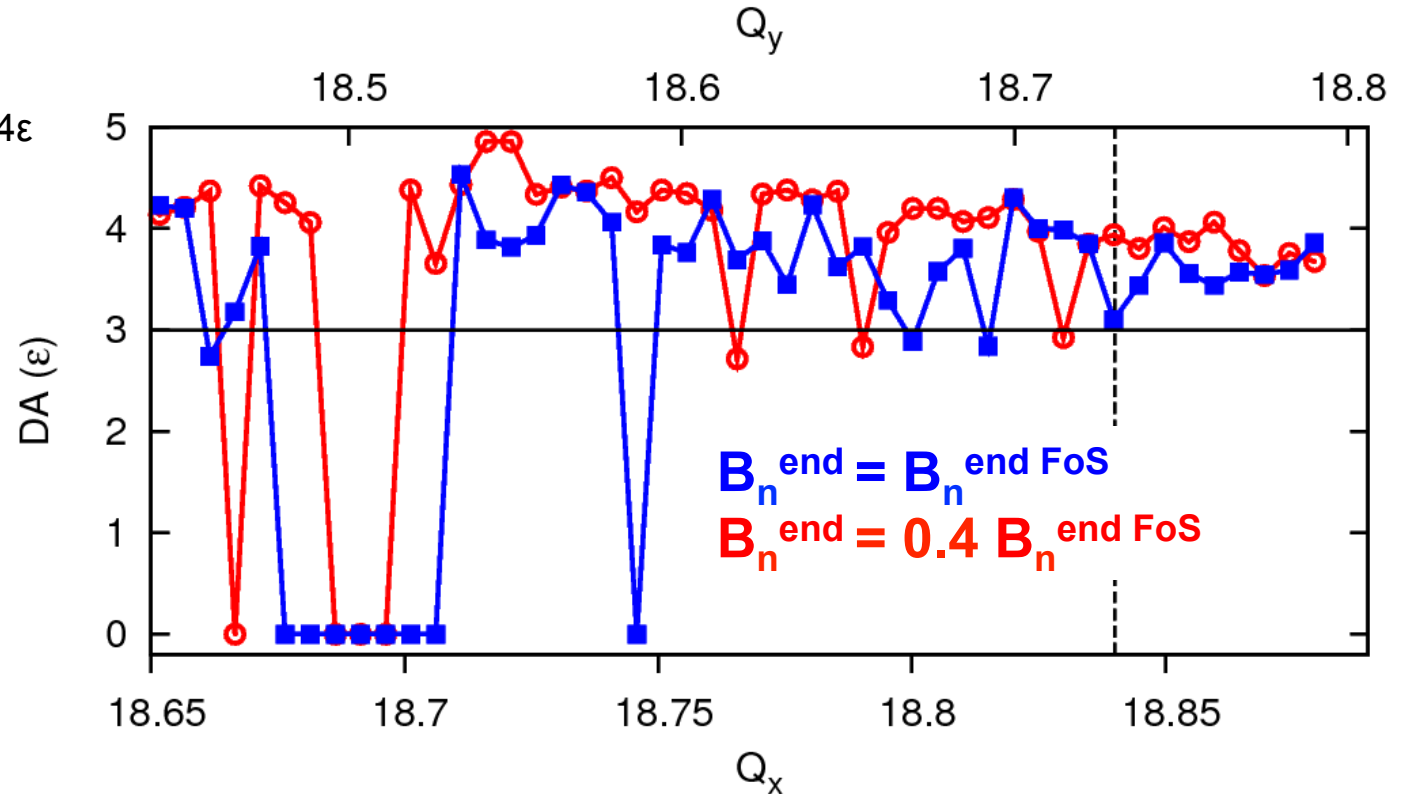
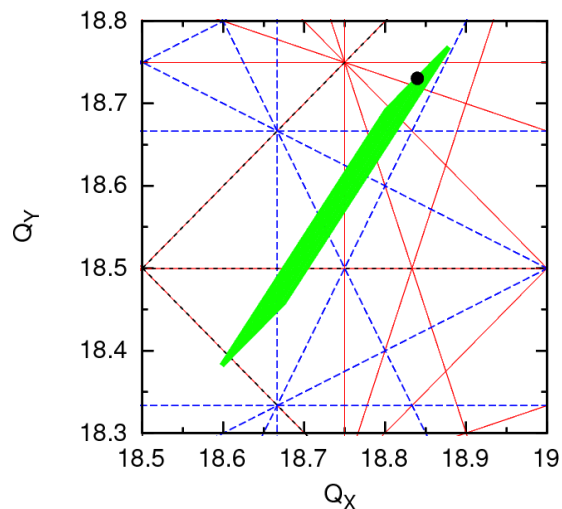
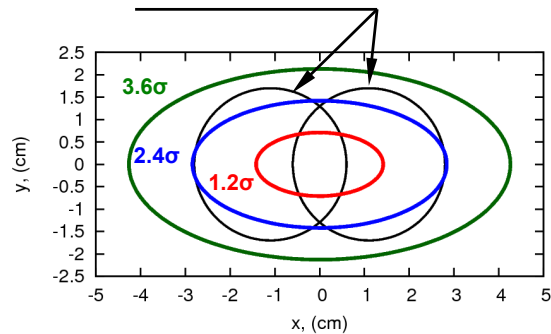
Beam $1\sigma = 11.8\text{mm}$ (hor)
 Measurement area $\approx 2.4\sigma \rightarrow 1.4\epsilon$
 Measurement coil: $r=1.7\text{cm}$



- Dipole Magnets: FoS $n \leq 7$; Quadrupoles: Comp. Model
- $\delta B_n = 0.3 B_n$
- Closed-Orbit: $\Delta x_{\text{rms}} = 1.5\text{mm}$, $\Delta y_{\text{rms}} = 1.0\text{mm}$
- 10^3 -turn scans with MADX, $\epsilon = 35\text{ mm mrad} \rightarrow 2\sigma$
- Tunes, chromaticity compensated
- No Space-Charge, no synchrotron motion

DYNAMIC APERTURE SCANS

Beam $1\sigma = 11.8\text{mm}$ (hor)
 Measurement area $\approx 2.4\sigma \rightarrow 1.4\epsilon$
 Measurement coil: $r=1.7\text{cm}$



If the magnetic field errors are strong like $\mathbf{B}_n^{\text{systr}}$ and vary like $\mathbf{B}_n^{\text{random}} = 0.3 \mathbf{B}_n^{\text{systr}}$, strong numerous resonances are excited.

Smaller systematic errors $\mathbf{B}_n^{\text{systr}}$ (end-block optimization, etc.) or smaller spreads will improve the single-particle stability

RESONANCES, OTHER OPERATIONS

Protons Low γ_t

$$Q_{X0} = 10.4$$

$$Q_{Y0} = 10.3$$

B2: normal quadrupole



A2: skew quadrupole

B3: normal sextupole

A3: skew sextupole

B4: normal octupole

A4: skew octupole

 coupling sum
 coupling difference

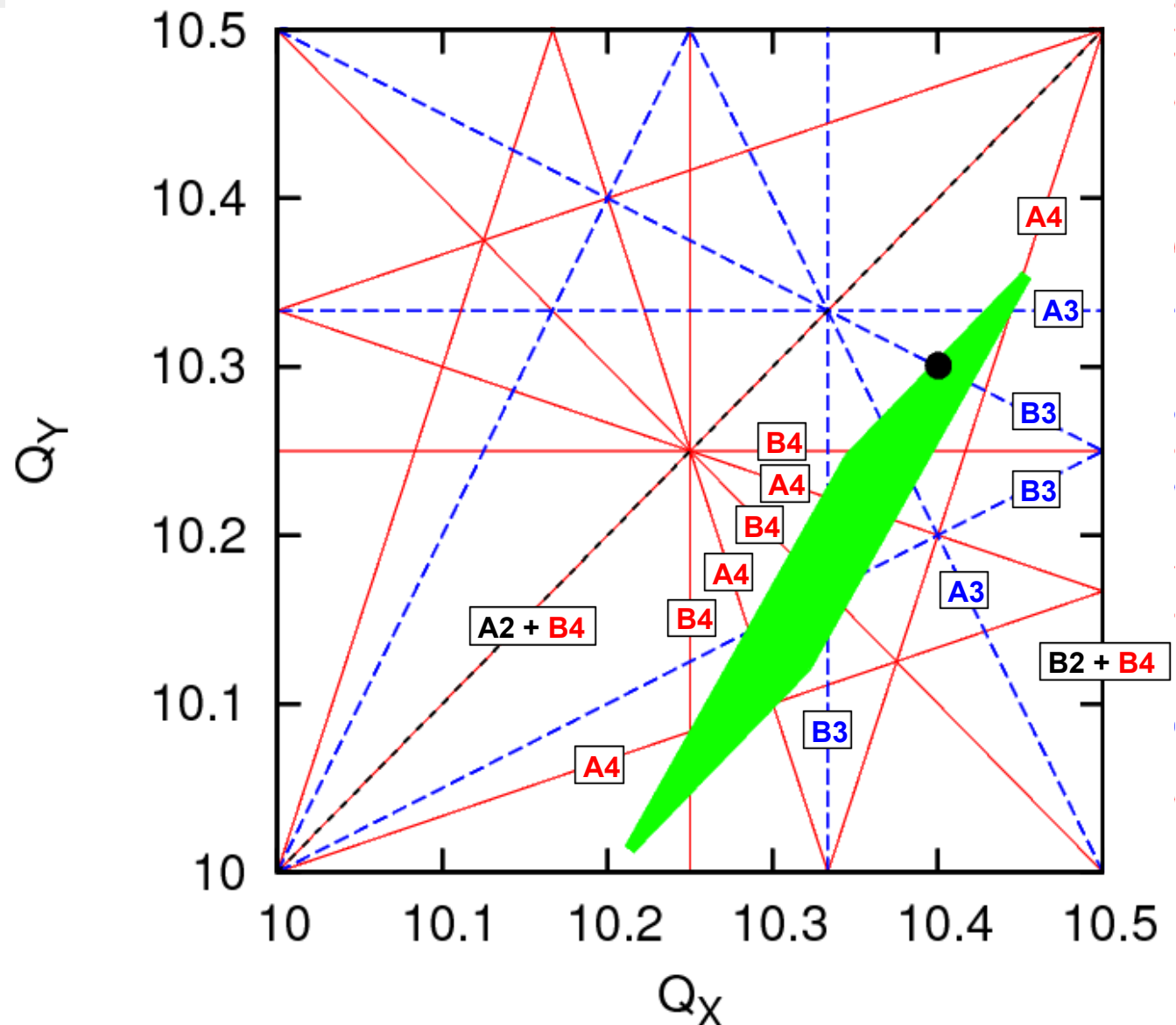
Additionally:

- Ions Slow Extraction

$$Q_{X0} = 17.3, Q_{Y0} = 17.8$$

- Protons High γ_t

$$Q_{X0} = 21.8, Q_{Y0} = 17.7$$



UPCOMING ACTIVITY

For a reliable assessment of the magnetic field quality, DA scans and the **beam loss calculations** with space charge are necessary, for Working Points of different operations. For this, the random error multipoles δB_n , δA_n are needed (from measurements or from simulations)

The (B_n, A_n) -measurements of the series magnets are essential:

- will provide the random errors
 - will be used for e.g. optimized chromaticity correction, resonance compensation, CO correction
 - needed for the commissioning
 - will be extensively used in the future 50 operation years
- 10%–20% of the series magnets are expected to be measured.

The workflow for the series magnetic data is under preparation. Simulations/Theory development for Beam Loss Studies is under progress.